## Chapter 3

## PROPERTIES OF PURE SUBSTANCES

We start this chapter with the introduction of the concept of a pure substance and a discussion of the physics of phase-change processes. We then illustrate the various property diagrams and $P-v-T$ surfaces of pure substances. After demonstrating the use of the property tables, the hypothetical substance ideal gas and the ideal-gas equation of state are discussed. The compressibility factor, which accounts for the deviation of real gases from ideal-gas behavior, is introduced, and some of the best-known equations of state such as the van der Waals, Beattie-Bridgeman, and Benedict-Webb-Rubin equations are presented.

## Objectives

The objectives of Chapter 3 are to:

- Introduce the concept of a pure substance.
- Discuss the physics of phase-change processes.
- Illustrate the $P-v, T-v$, and $P-T$ property diagrams and $P-v-T$ surfaces of pure substances.
- Demonstrate the procedures for determining thermodynamic properties of pure substances from tables of property data.
- Describe the hypothetical substance "ideal gas" and the ideal-gas equation of state.
- Apply the ideal-gas equation of state in the solution of typical problems.
- Introduce the compressibility factor, which accounts for the deviation of real gases from ideal-gas behavior.
- Present some of the best-known equations of state.


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FIGURE 3-1
Nitrogen and gaseous air are pure substances.


FIGURE 3-2
A mixture of liquid and gaseous water is a pure substance, but a mixture of liquid and gaseous air is not.

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FIGURE 3-3
The molecules in a solid are kept at their positions by the large springlike intermolecular forces.

## 3-1 • PURE SUBSTANCE

A substance that has a fixed chemical composition throughout is called a pure substance. Water, nitrogen, helium, and carbon dioxide, for example, are all pure substances.

A pure substance does not have to be of a single chemical element or compound, however. A mixture of various chemical elements or compounds also qualifies as a pure substance as long as the mixture is homogeneous. Air, for example, is a mixture of several gases, but it is often considered to be a pure substance because it has a uniform chemical composition (Fig. 3-1). However, a mixture of oil and water is not a pure substance. Since oil is not soluble in water, it will collect on top of the water, forming two chemically dissimilar regions.

A mixture of two or more phases of a pure substance is still a pure substance as long as the chemical composition of all phases is the same (Fig. 3-2). A mixture of ice and liquid water, for example, is a pure substance because both phases have the same chemical composition. A mixture of liquid air and gaseous air, however, is not a pure substance since the composition of liquid air is different from the composition of gaseous air, and thus the mixture is no longer chemically homogeneous. This is due to different components in air condensing at different temperatures at a specified pressure.

## 3-2 • PHASES OF A PURE SUBSTANCE

We all know from experience that substances exist in different phases. At room temperature and pressure, copper is a solid, mercury is a liquid, and nitrogen is a gas. Under different conditions, each may appear in a different phase. Even though there are three principal phases-solid, liquid, and gas-a substance may have several phases within a principal phase, each with a different molecular structure. Carbon, for example, may exist as graphite or diamond in the solid phase. Helium has two liquid phases; iron has three solid phases. Ice may exist at seven different phases at high pressures. A phase is identified as having a distinct molecular arrangement that is homogeneous throughout and separated from the others by easily identifiable boundary surfaces. The two phases of $\mathrm{H}_{2} \mathrm{O}$ in iced water represent a good example of this.
When studying phases or phase changes in thermodynamics, one does not need to be concerned with the molecular structure and behavior of different phases. However, it is very helpful to have some understanding of the molecular phenomena involved in each phase, and a brief discussion of phase transformations follows.

Intermolecular bonds are strongest in solids and weakest in gases. One reason is that molecules in solids are closely packed together, whereas in gases they are separated by relatively large distances.
The molecules in a solid are arranged in a three-dimensional pattern (lattice) that is repeated throughout (Fig. 3-3). Because of the small distances between molecules in a solid, the attractive forces of molecules on each other are large and keep the molecules at fixed positions (Fig. 3-4). Note that the attractive forces between molecules turn to repulsive forces as the
distance between the molecules approaches zero, thus preventing the molecules from piling up on top of each other. Even though the molecules in a solid cannot move relative to each other, they continually oscillate about their equilibrium positions. The velocity of the molecules during these oscillations depends on the temperature. At sufficiently high temperatures, the velocity (and thus the momentum) of the molecules may reach a point where the intermolecular forces are partially overcome and groups of molecules break away (Fig. 3-5). This is the beginning of the melting process.

The molecular spacing in the liquid phase is not much different from that of the solid phase, except the molecules are no longer at fixed positions relative to each other and they can rotate and translate freely. In a liquid, the intermolecular forces are weaker relative to solids, but still relatively strong compared with gases. The distances between molecules generally experience a slight increase as a solid turns liquid, with water being a notable exception.

In the gas phase, the molecules are far apart from each other, and a molecular order is nonexistent. Gas molecules move about at random, continually colliding with each other and the walls of the container they are in. Particularly at low densities, the intermolecular forces are very small, and collisions are the only mode of interaction between the molecules. Molecules in the gas phase are at a considerably higher energy level than they are in the liquid or solid phases. Therefore, the gas must release a large amount of its energy before it can condense or freeze.

## 3-3 • PHASE-CHANGE PROCESSES OF PURE SUBSTANCES

There are many practical situations where two phases of a pure substance coexist in equilibrium. Water exists as a mixture of liquid and vapor in the boiler and the condenser of a steam power plant. The refrigerant turns from liquid to vapor in the freezer of a refrigerator. Even though many home owners consider the freezing of water in underground pipes as the most


FIGURE 3-4
In a solid, the attractive and repulsive forces between the molecules tend to maintain them at relatively constant distances from each other.
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FIGURE 3-5
The arrangement of atoms in different phases: (a) molecules are at relatively fixed positions in a solid, (b) groups of molecules move about each other in the liquid phase, and (c) molecules move about at random in the gas phase.

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FIGURE 3-6
At 1 atm and $20^{\circ} \mathrm{C}$, water exists in the liquid phase (compressed liquid).


FIGURE 3-7
At 1 atm pressure and $100^{\circ} \mathrm{C}$, water exists as a liquid that is ready to vaporize (saturated liquid).


FIGURE 3-8
As more heat is transferred, part of the saturated liquid vaporizes (saturated liquid-vapor mixture).
important phase-change process, attention in this section is focused on the liquid and vapor phases and their mixture. As a familiar substance, water is used to demonstrate the basic principles involved. Remember, however, that all pure substances exhibit the same general behavior.

## Compressed Liquid and Saturated Liquid

Consider a piston-cylinder device containing liquid water at $20^{\circ} \mathrm{C}$ and 1 atm pressure (state 1, Fig. 3-6). Under these conditions, water exists in the liquid phase, and it is called a compressed liquid, or a subcooled liquid, meaning that it is not about to vaporize. Heat is now transferred to the water until its temperature rises to, say, $40^{\circ} \mathrm{C}$. As the temperature rises, the liquid water expands slightly, and so its specific volume increases. To accommodate this expansion, the piston moves up slightly. The pressure in the cylinder remains constant at 1 atm during this process since it depends on the outside barometric pressure and the weight of the piston, both of which are constant. Water is still a compressed liquid at this state since it has not started to vaporize.
As more heat is transferred, the temperature keeps rising until it reaches $100^{\circ} \mathrm{C}$ (state 2, Fig. 3-7). At this point water is still a liquid, but any heat addition will cause some of the liquid to vaporize. That is, a phase-change process from liquid to vapor is about to take place. A liquid that is about to vaporize is called a saturated liquid. Therefore, state 2 is a saturated liquid state.

## Saturated Vapor and Superheated Vapor

Once boiling starts, the temperature stops rising until the liquid is completely vaporized. That is, the temperature will remain constant during the entire phase-change process if the pressure is held constant. This can easily be verified by placing a thermometer into boiling pure water on top of a stove. At sea level $(P=1 \mathrm{~atm})$, the thermometer will always read $100^{\circ} \mathrm{C}$ if the pan is uncovered or covered with a light lid. During a boiling process, the only change we will observe is a large increase in the volume and a steady decline in the liquid level as a result of more liquid turning to vapor.
Midway about the vaporization line (state 3, Fig. 3-8), the cylinder contains equal amounts of liquid and vapor. As we continue transferring heat, the vaporization process continues until the last drop of liquid is vaporized (state 4, Fig. 3-9). At this point, the entire cylinder is filled with vapor that is on the borderline of the liquid phase. Any heat loss from this vapor will cause some of the vapor to condense (phase change from vapor to liquid). A vapor that is about to condense is called a saturated vapor. Therefore, state 4 is a saturated vapor state. A substance at states between 2 and 4 is referred to as a saturated liquid-vapor mixture since the liquid and vapor phases coexist in equilibrium at these states.

Once the phase-change process is completed, we are back to a singlephase region again (this time vapor), and further transfer of heat results in an increase in both the temperature and the specific volume (Fig. 3-10). At state 5 , the temperature of the vapor is, let us say, $300^{\circ} \mathrm{C}$; and if we transfer some heat from the vapor, the temperature may drop somewhat but no condensation will take place as long as the temperature remains above $100^{\circ} \mathrm{C}$
(for $P=1 \mathrm{~atm}$ ). A vapor that is not about to condense (i.e., not a saturated vapor) is called a superheated vapor. Therefore, water at state 5 is a superheated vapor. This constant-pressure phase-change process is illustrated on a $T-V$ diagram in Fig. 3-11.

If the entire process described here is reversed by cooling the water while maintaining the pressure at the same value, the water will go back to state 1 , retracing the same path, and in so doing, the amount of heat released will exactly match the amount of heat added during the heating process.

In our daily life, water implies liquid water and steam implies water vapor. In thermodynamics, however, both water and steam usually mean only one thing: $\mathrm{H}_{2} \mathrm{O}$.

## Saturation Temperature and Saturation Pressure

It probably came as no surprise to you that water started to boil at $100^{\circ} \mathrm{C}$. Strictly speaking, the statement "water boils at $100^{\circ} \mathrm{C}$ " is incorrect. The correct statement is "water boils at $100^{\circ} \mathrm{C}$ at 1 atm pressure." The only reason water started boiling at $100^{\circ} \mathrm{C}$ was because we held the pressure constant at $1 \mathrm{~atm}(101.325 \mathrm{kPa})$. If the pressure inside the cylinder were raised to 500 kPa by adding weights on top of the piston, water would start boiling at $151.8^{\circ} \mathrm{C}$. That is, the temperature at which water starts boiling depends on the pressure; therefore, if the pressure is fixed, so is the boiling temperature.

At a given pressure, the temperature at which a pure substance changes phase is called the saturation temperature $T_{\text {sat }}$. Likewise, at a given temperature, the pressure at which a pure substance changes phase is called the saturation pressure $P_{\text {sat }}$. At a pressure of $101.325 \mathrm{kPa}, T_{\text {sat }}$ is $99.97^{\circ} \mathrm{C}$. Conversely, at a temperature of $99.97^{\circ} \mathrm{C}, P_{\text {sat }}$ is 101.325 kPa . (At $100.00^{\circ} \mathrm{C}$, $P_{\text {sat }}$ is 101.42 kPa in the ITS-90 discussed in Chap. 1.)

Saturation tables that list the saturation pressure against the temperature (or the saturation temperature against the pressure) are available for


FIGURE 3-11
$T-\vee$ diagram for the heating process of water at constant pressure.


FIGURE 3-9
At 1 atm pressure, the temperature remains constant at $100^{\circ} \mathrm{C}$ until the last drop of liquid is vaporized (saturated vapor).


FIGURE 3-10
As more heat is transferred, the temperature of the vapor starts to rise (superheated vapor).

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EXPERIMENT


Use actual data from the experiment shown here to obtain the latent heat of fusion of water. See end-of-chapter problem 3-146.

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| :--- | :---: |
|  |  |
|  |  |
|  |  |
| TABLE 3-1 | Saturation |
| Saturation (boiling) pressure of |  |
| water at various temperatures |  |
|  | pressure, |
| Temperature, | $P_{\text {sat }}$, kPa |
| $T,{ }^{\circ} \mathrm{C}$ | 0.26 |
| 10 | 0.40 |
| -5 | 0.61 |
| 0 | 0.87 |
| 5 | 1.23 |
| 10 | 1.71 |
| 15 | 2.34 |
| 20 | 3.17 |
| 25 | 4.25 |
| 30 | 7.39 |
| 40 | 12.35 |
| 50 | 101.4 |
| 100 | 476.2 |
| 150 | 1555 |
| 200 | 3976 |
| 250 | 8588 |
| 300 |  |

FIGURE 3-12
The liquid-vapor saturation curve of a pure substance (numerical values are for water).
practically all substances. A partial listing of such a table is given in Table 3-1 for water. This table indicates that the pressure of water changing phase (boiling or condensing) at $25^{\circ} \mathrm{C}$ must be 3.17 kPa , and the pressure of water must be maintained at 3976 kPa (about 40 atm ) to have it boil at $250^{\circ} \mathrm{C}$. Also, water can be frozen by dropping its pressure below 0.61 kPa .

It takes a large amount of energy to melt a solid or vaporize a liquid. The amount of energy absorbed or released during a phase-change process is called the latent heat. More specifically, the amount of energy absorbed during melting is called the latent heat of fusion and is equivalent to the amount of energy released during freezing. Similarly, the amount of energy absorbed during vaporization is called the latent heat of vaporization and is equivalent to the energy released during condensation. The magnitudes of the latent heats depend on the temperature or pressure at which the phase change occurs. At 1 atm pressure, the latent heat of fusion of water is 333.7 $\mathrm{kJ} / \mathrm{kg}$ and the latent heat of vaporization is $2256.5 \mathrm{~kJ} / \mathrm{kg}$.

During a phase-change process, pressure and temperature are obviously dependent properties, and there is a definite relation between them, that is, $T_{\text {sat }}=f\left(P_{\text {sat }}\right)$. A plot of $T_{\text {sat }}$ versus $P_{\text {sat }}$, such as the one given for water in Fig. 3-12, is called a liquid-vapor saturation curve. A curve of this kind is characteristic of all pure substances.
It is clear from Fig. 3-12 that $T_{\text {sat }}$ increases with $P_{\text {sat }}$. Thus, a substance at higher pressures boils at higher temperatures. In the kitchen, higher boiling temperatures mean shorter cooking times and energy savings. A beef stew, for example, may take 1 to 2 h to cook in a regular pan that operates at 1 atm pressure, but only 20 min in a pressure cooker operating at 3 atm absolute pressure (corresponding boiling temperature: $134^{\circ} \mathrm{C}$ ).

The atmospheric pressure, and thus the boiling temperature of water, decreases with elevation. Therefore, it takes longer to cook at higher altitudes than it does at sea level (unless a pressure cooker is used). For example, the standard atmospheric pressure at an elevation of 2000 m is 79.50 kPa , which corresponds to a boiling temperature of $93.3^{\circ} \mathrm{C}$ as opposed to $100^{\circ} \mathrm{C}$ at sea level (zero elevation). The variation of the boiling temperature of water with altitude at standard atmospheric conditions is given in Table 3-2. For each 1000 m increase in elevation, the boiling temperature

drops by a little over $3^{\circ} \mathrm{C}$. Note that the atmospheric pressure at a location, and thus the boiling temperature, changes slightly with the weather conditions. But the corresponding change in the boiling temperature is no more than about $1^{\circ} \mathrm{C}$.

## Some Consequences of $T_{\text {sat }}$ and $P_{\text {sat }}$ Dependence

We mentioned earlier that a substance at a specified pressure boils at the saturation temperature corresponding to that pressure. This phenomenon allows us to control the boiling temperature of a substance by simply controlling the pressure, and it has numerous applications in practice. Below we give some examples. The natural drive to achieve phase equilibrium by allowing some liquid to evaporate is at work behind the scenes.

Consider a sealed can of liquid refrigerant-134a in a room at $25^{\circ} \mathrm{C}$. If the can has been in the room long enough, the temperature of the refrigerant in the can is also $25^{\circ} \mathrm{C}$. Now, if the lid is opened slowly and some refrigerant is allowed to escape, the pressure in the can will start dropping until it reaches the atmospheric pressure. If you are holding the can, you will notice its temperature dropping rapidly, and even ice forming outside the can if the air is humid. A thermometer inserted in the can will register $-26^{\circ} \mathrm{C}$ when the pressure drops to 1 atm , which is the saturation temperature of refriger-ant-134a at that pressure. The temperature of the liquid refrigerant will remain at $-26^{\circ} \mathrm{C}$ until the last drop of it vaporizes.

Another aspect of this interesting physical phenomenon is that a liquid cannot vaporize unless it absorbs energy in the amount of the latent heat of vaporization, which is $217 \mathrm{~kJ} / \mathrm{kg}$ for refrigerant-134a at 1 atm . Therefore, the rate of vaporization of the refrigerant depends on the rate of heat transfer to the can: the larger the rate of heat transfer, the higher the rate of vaporization. The rate of heat transfer to the can and thus the rate of vaporization of the refrigerant can be minimized by insulating the can heavily. In the limiting case of no heat transfer, the refrigerant will remain in the can as a liquid at $-26^{\circ} \mathrm{C}$ indefinitely.

The boiling temperature of nitrogen at atmospheric pressure is $-196^{\circ} \mathrm{C}$ (see Table $\mathrm{A}-3 a$ ). This means the temperature of liquid nitrogen exposed to the atmosphere must be $-196^{\circ} \mathrm{C}$ since some nitrogen will be evaporating. The temperature of liquid nitrogen remains constant at $-196^{\circ} \mathrm{C}$ until it is depleted. For this reason, nitrogen is commonly used in low-temperature scientific studies (such as superconductivity) and cryogenic applications to maintain a test chamber at a constant temperature of $-196^{\circ} \mathrm{C}$. This is done by placing the test chamber into a liquid nitrogen bath that is open to the atmosphere. Any heat transfer from the environment to the test section is absorbed by the nitrogen, which evaporates isothermally and keeps the test chamber temperature constant at $-196^{\circ} \mathrm{C}$ (Fig. 3-13). The entire test section must be insulated heavily to minimize heat transfer and thus liquid nitrogen consumption. Liquid nitrogen is also used for medical purposes to burn off unsightly spots on the skin. This is done by soaking a cotton swap in liquid nitrogen and wetting the target area with it. As the nitrogen evaporates, it freezes the affected skin by rapidly absorbing heat from it.

A practical way of cooling leafy vegetables is vacuum cooling, which is based on reducing the pressure of the sealed cooling chamber to the saturation pressure at the desired low temperature, and evaporating some water

## TABLE 3-2

Variation of the standard atmospheric pressure and the boiling (saturation) temperature of water with altitude

| Elevation, <br> m | Atmospheric <br> pressure, | Boiling <br> tempera- <br> ture, |
| ---: | ---: | ---: |
| 0 |  |  | | $\circ$ |
| ---: | ---: | ---: |



FIGURE 3-13
The temperature of liquid nitrogen exposed to the atmosphere remains constant at $-196^{\circ} \mathrm{C}$, and thus it maintains the test chamber at $-196^{\circ} \mathrm{C}$.

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FIGURE 3-14
The variation of the temperature of fruits and vegetables with pressure during vacuum cooling from $25^{\circ} \mathrm{C}$ to $0^{\circ} \mathrm{C}$.


FIGURE 3-15
In 1775 , ice was made by evacuating the air space in a water tank.
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from the products to be cooled. The heat of vaporization during evaporation is absorbed from the products, which lowers the product temperature. The saturation pressure of water at $0^{\circ} \mathrm{C}$ is 0.61 kPa , and the products can be cooled to $0^{\circ} \mathrm{C}$ by lowering the pressure to this level. The cooling rate can be increased by lowering the pressure below 0.61 kPa , but this is not desirable because of the danger of freezing and the added cost.
In vacuum cooling, there are two distinct stages. In the first stage, the products at ambient temperature, say at $25^{\circ} \mathrm{C}$, are loaded into the chamber, and the operation begins. The temperature in the chamber remains constant until the saturation pressure is reached, which is 3.17 kPa at $25^{\circ} \mathrm{C}$. In the second stage that follows, saturation conditions are maintained inside at progressively lower pressures and the corresponding lower temperatures until the desired temperature is reached (Fig. 3-14).

Vacuum cooling is usually more expensive than the conventional refrigerated cooling, and its use is limited to applications that result in much faster cooling. Products with large surface area per unit mass and a high tendency to release moisture such as lettuce and spinach are well-suited for vacuum cooling. Products with low surface area to mass ratio are not suitable, especially those that have relatively impervious peels such as tomatoes and cucumbers. Some products such as mushrooms and green peas can be vacuum cooled successfully by wetting them first.
The vacuum cooling just described becomes vacuum freezing if the vapor pressure in the vacuum chamber is dropped below 0.61 kPa , the saturation pressure of water at $0^{\circ} \mathrm{C}$. The idea of making ice by using a vacuum pump is nothing new. Dr. William Cullen actually made ice in Scotland in 1775 by evacuating the air in a water tank (Fig. 3-15).

Package icing is commonly used in small-scale cooling applications to remove heat and keep the products cool during transit by taking advantage of the large latent heat of fusion of water, but its use is limited to products that are not harmed by contact with ice. Also, ice provides moisture as well as refrigeration.

## 3-4 • PROPERTY DIAGRAMS FOR PHASE-CHANGE PROCESSES

The variations of properties during phase-change processes are best studied and understood with the help of property diagrams. Next, we develop and discuss the $T-V, P-V$, and $P-T$ diagrams for pure substances.

## 1 The T-v Diagram

The phase-change process of water at 1 atm pressure was described in detail in the last section and plotted on a $T-v$ diagram in Fig. 3-11. Now we repeat this process at different pressures to develop the $T-\vee$ diagram.

Let us add weights on top of the piston until the pressure inside the cylinder reaches 1 MPa . At this pressure, water has a somewhat smaller specific volume than it does at 1 atm pressure. As heat is transferred to the water at this new pressure, the process follows a path that looks very much like the process path at 1 atm pressure, as shown in Fig. 3-16, but there are some noticeable differences. First, water starts boiling at a much higher tempera-


FIGURE 3-16
$T-v$ diagram of constant-pressure phase-change processes of a pure substance at various pressures (numerical values are for water).
ture $\left(179.9^{\circ} \mathrm{C}\right)$ at this pressure. Second, the specific volume of the saturated liquid is larger and the specific volume of the saturated vapor is smaller than the corresponding values at 1 atm pressure. That is, the horizontal line that connects the saturated liquid and saturated vapor states is much shorter.

As the pressure is increased further, this saturation line continues to shrink, as shown in Fig. 3-16, and it becomes a point when the pressure reaches 22.06 MPa for the case of water. This point is called the critical point, and it is defined as the point at which the saturated liquid and saturated vapor states are identical.

The temperature, pressure, and specific volume of a substance at the critical point are called, respectively, the critical temperature $T_{\mathrm{cr}}$, critical pressure $P_{\mathrm{cr}}$, and critical specific volume $V_{\mathrm{cr}}$. The critical-point properties of water are $P_{\mathrm{cr}}=22.06 \mathrm{MPa}, T_{\mathrm{cr}}=373.95^{\circ} \mathrm{C}$, and ${V_{\mathrm{cr}}}=0.003106 \mathrm{~m}^{3} / \mathrm{kg}$. For helium, they are $0.23 \mathrm{MPa},-267.85^{\circ} \mathrm{C}$, and $0.01444 \mathrm{~m}^{3} / \mathrm{kg}$. The critical properties for various substances are given in Table A-1 in the appendix.

At pressures above the critical pressure, there is not a distinct phasechange process (Fig. 3-17). Instead, the specific volume of the substance continually increases, and at all times there is only one phase present. Eventually, it resembles a vapor, but we can never tell when the change


FIGURE 3-17
At supercritical pressures $\left(P>P_{\text {cr }}\right)$, there is no distinct phase-change (boiling) process.

FIGURE 3-18
$T-\cup$ diagram of a pure substance.
has occurred. Above the critical state, there is no line that separates the compressed liquid region and the superheated vapor region. However, it is customary to refer to the substance as superheated vapor at temperatures above the critical temperature and as compressed liquid at temperatures below the critical temperature.

The saturated liquid states in Fig. 3-16 can be connected by a line called the saturated liquid line, and saturated vapor states in the same figure can be connected by another line, called the saturated vapor line. These two lines meet at the critical point, forming a dome as shown in Fig. 3-18. All the compressed liquid states are located in the region to the left of the saturated liquid line, called the compressed liquid region. All the superheated vapor states are located to the right of the saturated vapor line, called the superheated vapor region. In these two regions, the substance exists in a single phase, a liquid or a vapor. All the states that involve both phases in equilibrium are located under the dome, called the saturated liquid-vapor mixture region, or the wet region.

## 2 The P-v Diagram

The general shape of the $P-\vee$ diagram of a pure substance is very much like the $T-v$ diagram, but the $T=$ constant lines on this diagram have a downward trend, as shown in Fig. 3-19.

Consider again a piston-cylinder device that contains liquid water at 1 MPa and $150^{\circ} \mathrm{C}$. Water at this state exists as a compressed liquid. Now the weights on top of the piston are removed one by one so that the pressure inside the cylinder decreases gradually (Fig. 3-20). The water is allowed to exchange heat with the surroundings so its temperature remains constant. As


the pressure decreases, the volume of the water increases slightly. When the pressure reaches the saturation-pressure value at the specified temperature $(0.4762 \mathrm{MPa})$, the water starts to boil. During this vaporization process, both the temperature and the pressure remain constant, but the specific volume increases. Once the last drop of liquid is vaporized, further reduction in pressure results in a further increase in specific volume. Notice that during the phase-change process, we did not remove any weights. Doing so would cause the pressure and therefore the temperature to drop [since $T_{\text {sat }}=$ $f\left(P_{\text {sat }}\right)$, and the process would no longer be isothermal.

When the process is repeated for other temperatures, similar paths are obtained for the phase-change processes. Connecting the saturated liquid and the saturated vapor states by a curve, we obtain the $P-\vee$ diagram of a pure substance, as shown in Fig. 3-19.

## Extending the Diagrams to Include the Solid Phase

The two equilibrium diagrams developed so far represent the equilibrium states involving the liquid and the vapor phases only. However, these diagrams can easily be extended to include the solid phase as well as the solid-liquid and the solid-vapor saturation regions. The basic principles discussed in conjunction with the liquid-vapor phase-change process apply equally to the solid-liquid and solid-vapor phase-change processes. Most substances contract during a solidification (i.e., freezing) process. Others, like water, expand as they freeze. The $P-\vee$ diagrams for both groups of substances are given in Figs. 3-21 and 3-22. These two diagrams differ only in

FIGURE 3-19
$P-\vee$ diagram of a pure substance.


FIGURE 3-20
The pressure in a piston-cylinder device can be reduced by reducing the weight of the piston.

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## FIGURE 3-21

$P-\vee$ diagram of a substance that contracts on freezing.

## FIGURE 3-22

$P-\vee$ diagram of a substance that expands on freezing (such as water).


the solid-liquid saturation region. The $T-v$ diagrams look very much like the $P-V$ diagrams, especially for substances that contract on freezing.

The fact that water expands upon freezing has vital consequences in nature. If water contracted on freezing as most other substances do, the ice formed would be heavier than the liquid water, and it would settle to the bottom of rivers, lakes, and oceans instead of floating at the top. The sun's
rays would never reach these ice layers, and the bottoms of many rivers, lakes, and oceans would be covered with ice at times, seriously disrupting marine life.

We are all familiar with two phases being in equilibrium, but under some conditions all three phases of a pure substance coexist in equilibrium (Fig. 3-23). On $P-V$ or $T-V$ diagrams, these triple-phase states form a line called the triple line. The states on the triple line of a substance have the same pressure and temperature but different specific volumes. The triple line appears as a point on the $P-T$ diagrams and, therefore, is often called the triple point. The triple-point temperatures and pressures of various substances are given in Table 3-3. For water, the triple-point temperature and pressure are $0.01^{\circ} \mathrm{C}$ and 0.6117 kPa , respectively. That is, all three phases of water coexist in equilibrium only if the temperature and pressure have precisely these values. No substance can exist in the liquid phase in stable equilibrium at pressures below the triple-point pressure. The same can be said for temperature for substances that contract on freezing. However,


FIGURE 3-23
At triple-point pressure and temperature, a substance exists in three phases in equilibrium.

## TABLE 3-3

Triple-point temperatures and pressures of various substances

| Substance | Formula | $T_{\mathrm{tp}}, \mathrm{K}$ | $P_{\mathrm{tp}}, \mathrm{kPa}$ |
| :--- | :--- | :---: | :---: |
| Acetylene | $\mathrm{C}_{2} \mathrm{H}_{2}$ | 192.4 | 120 |
| Ammonia | $\mathrm{NH}_{3}$ | 195.40 | 6.076 |
| Argon | A | 83.81 | 68.9 |
| Carbon (graphite) | C | 3900 | 10,100 |
| Carbon dioxide | $\mathrm{CO}_{2}$ | 216.55 | 517 |
| Carbon monoxide | $\mathrm{CO}_{2}$ | 68.10 | 15.37 |
| Deuterium | $\mathrm{D}_{2}$ | 18.63 | 17.1 |
| Ethane | $\mathrm{C}_{2} \mathrm{H}_{6}$ | 89.89 | $8 \times 10^{-4}$ |
| Ethylene | $\mathrm{C}_{2} \mathrm{H}_{4}$ | 104.0 | 0.12 |
| Helium 4 ( $\lambda$ point) | $\mathrm{He}^{2}$ | 2.19 | 5.1 |
| Hydrogen | $\mathrm{H}_{2}$ | 13.84 | 7.04 |
| Hydrogen chloride | HCl | 158.96 | 13.9 |
| Mercury | Hg | 234.2 | $1.65 \times 10^{-7}$ |
| Methane | CH | 90.68 | 11.7 |
| Neon | Ne | 24.57 | 43.2 |
| Nitric oxide | NO | 109.50 | 21.92 |
| Nitrogen | $\mathrm{N}_{2}$ | 63.18 | 12.6 |
| Nitrous oxide | $\mathrm{N}_{2} \mathrm{O}$ | 182.34 | 87.85 |
| Oxygen | $\mathrm{O}_{2}$ | 54.36 | 0.152 |
| Palladium | Pd | 1825 | $3.5 \times 10^{-3}$ |
| Platinum | Pt | 2045 | $2.0 \times 10^{-4}$ |
| Sulfur dioxide | $\mathrm{SO}_{2}$ | 197.69 | 1.67 |
| Titanium | Ti | 1941 | $5.3 \times 10^{-3}$ |
| Uranium hexafluoride | $\mathrm{UF}_{6}$ | 337.17 | 151.7 |
| Water | $\mathrm{H}_{2} \mathrm{O}$ | 273.16 | 0.61 |
| Xenon | Xe | 161.3 | 81.5 |
| Zinc | Zn | 692.65 | 0.065 |

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FIGURE 3-24
At low pressures (below the triplepoint value), solids evaporate without melting first (sublimation).

FIGURE 3-25
$P-T$ diagram of pure substances.
substances at high pressures can exist in the liquid phase at temperatures below the triple-point temperature. For example, water cannot exist in liquid form in equilibrium at atmospheric pressure at temperatures below $0^{\circ} \mathrm{C}$, but it can exist as a liquid at $-20^{\circ} \mathrm{C}$ at 200 MPa pressure. Also, ice exists at seven different solid phases at pressures above 100 MPa .

There are two ways a substance can pass from the solid to vapor phase: either it melts first into a liquid and subsequently evaporates, or it evaporates directly without melting first. The latter occurs at pressures below the triplepoint value, since a pure substance cannot exist in the liquid phase at those pressures (Fig. 3-24). Passing from the solid phase directly into the vapor phase is called sublimation. For substances that have a triple-point pressure above the atmospheric pressure such as solid $\mathrm{CO}_{2}$ (dry ice), sublimation is the only way to change from the solid to vapor phase at atmospheric conditions.

## 3 The P-T Diagram

Figure $3-25$ shows the $P-T$ diagram of a pure substance. This diagram is often called the phase diagram since all three phases are separated from each other by three lines. The sublimation line separates the solid and vapor regions, the vaporization line separates the liquid and vapor regions, and the melting (or fusion) line separates the solid and liquid regions. These three lines meet at the triple point, where all three phases coexist in equilibrium. The vaporization line ends at the critical point because no distinction can be made between liquid and vapor phases above the critical point. Substances that expand and contract on freezing differ only in the melting line on the $P-T$ diagram.


## The $P$ - $v$ - $T$ Surface

The state of a simple compressible substance is fixed by any two independent, intensive properties. Once the two appropriate properties are fixed, all the other properties become dependent properties. Remembering that any equation with two independent variables in the form $z=z(x, y)$ represents a surface in space, we can represent the $P-V-T$ behavior of a substance as a surface in space, as shown in Figs. 3-26 and 3-27. Here $T$ and $v$ may be


FIGURE 3-26
$P-\mathrm{V}-T$ surface of a substance that contracts on freezing.

FIGURE 3-27
$P-\vee-T$ surface of a substance that expands on freezing (like water).


FIGURE 3-28
The combination $u+P \vee$ is frequently encountered in the analysis of control volumes.
viewed as the independent variables (the base) and $P$ as the dependent variable (the height).

All the points on the surface represent equilibrium states. All states along the path of a quasi-equilibrium process lie on the $P-v-T$ surface since such a process must pass through equilibrium states. The single-phase regions appear as curved surfaces on the $P-\vee-T$ surface, and the two-phase regions as surfaces perpendicular to the $P-T$ plane. This is expected since the projections of two-phase regions on the $P-T$ plane are lines.
All the two-dimensional diagrams we have discussed so far are merely projections of this three-dimensional surface onto the appropriate planes. A $P-V$ diagram is just a projection of the $P-V-T$ surface on the $P-\vee$ plane, and a $T-V$ diagram is nothing more than the bird's-eye view of this surface. The $P-v-T$ surfaces present a great deal of information at once, but in a thermodynamic analysis it is more convenient to work with two-dimensional diagrams, such as the $P-\vee$ and $T-\vee$ diagrams.

## 3-5 • PROPERTY TABLES

For most substances, the relationships among thermodynamic properties are too complex to be expressed by simple equations. Therefore, properties are frequently presented in the form of tables. Some thermodynamic properties can be measured easily, but others cannot and are calculated by using the relations between them and measurable properties. The results of these measurements and calculations are presented in tables in a convenient format. In the following discussion, the steam tables are used to demonstrate the use of thermodynamic property tables. Property tables of other substances are used in the same manner.

For each substance, the thermodynamic properties are listed in more than one table. In fact, a separate table is prepared for each region of interest such as the superheated vapor, compressed liquid, and saturated (mixture) regions. Property tables are given in the appendix in both SI and English units. The tables in English units carry the same number as the corresponding tables in SI, followed by an identifier E. Tables A-6 and A-6E, for example, list properties of superheated water vapor, the former in SI and the latter in English units. Before we get into the discussion of property tables, we define a new property called enthalpy.

## Enthalpy—A Combination Property

A person looking at the tables will notice two new properties: enthalpy $h$ and entropy $s$. Entropy is a property associated with the second law of thermodynamics, and we will not use it until it is properly defined in Chap. 7. However, it is appropriate to introduce enthalpy at this point.

In the analysis of certain types of processes, particularly in power generation and refrigeration (Fig. 3-28), we frequently encounter the combination of properties $u+P \vee$. For the sake of simplicity and convenience, this combination is defined as a new property, enthalpy, and given the symbol $h$ :

$$
\begin{equation*}
h=u+P v \quad(\mathrm{~kJ} / \mathrm{kg}) \tag{3-1}
\end{equation*}
$$

or,

$$
\begin{equation*}
H=U+P V \tag{kJ}
\end{equation*}
$$

Both the total enthalpy $H$ and specific enthalpy $h$ are simply referred to as enthalpy since the context clarifies which one is meant. Notice that the equations given above are dimensionally homogeneous. That is, the unit of the pressure-volume product may differ from the unit of the internal energy by only a factor (Fig. 3-29). For example, it can be easily shown that $1 \mathrm{kPa} \cdot \mathrm{m}^{3}=1 \mathrm{~kJ}$. In some tables encountered in practice, the internal energy $u$ is frequently not listed, but it can always be determined from $u=h-P v$.

The widespread use of the property enthalpy is due to Professor Richard Mollier, who recognized the importance of the group $u+P \vee$ in the analysis of steam turbines and in the representation of the properties of steam in tabular and graphical form (as in the famous Mollier chart). Mollier referred to the group $u+P \vee$ as heat content and total heat. These terms were not quite consistent with the modern thermodynamic terminology and were replaced in the 1930s by the term enthalpy (from the Greek word enthalpien, which means to heat).

## 1a Saturated Liquid and Saturated Vapor States

The properties of saturated liquid and saturated vapor for water are listed in Tables A-4 and A-5. Both tables give the same information. The only difference is that in Table A-4 properties are listed under temperature and in Table A-5 under pressure. Therefore, it is more convenient to use Table A-4 when temperature is given and Table A-5 when pressure is given. The use of Table A-4 is illustrated in Fig. 3-30.

The subscript $f$ is used to denote properties of a saturated liquid, and the subscript $g$ to denote the properties of saturated vapor. These symbols are commonly used in thermodynamics and originated from German. Another subscript commonly used is $f g$, which denotes the difference between the saturated vapor and saturated liquid values of the same property. For example,

$$
\begin{aligned}
v_{f} & =\text { specific volume of saturated liquid } \\
v_{g} & =\text { specific volume of saturated vapor } \\
v_{f g} & \left.=\text { difference between } v_{g} \text { and } v_{f} \text { (that is, } v_{f g}=v_{g}-v_{f}\right)
\end{aligned}
$$

The quantity $h_{f g}$ is called the enthalpy of vaporization (or latent heat of vaporization). It represents the amount of energy needed to vaporize a unit mass of saturated liquid at a given temperature or pressure. It decreases as the temperature or pressure increases and becomes zero at the critical point.


FIGURE 3-29
The product pressure $\times$ volume has energy units.


FIGURE 3-30
A partial list of Table A-4.

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FIGURE 3-31
Schematic and $T-\vee$ diagram for Example 3-1.


FIGURE 3-32
Schematic and $P-V$ diagram for Example 3-2.

## EXAMPLE 3-1 Pressure of Saturated Liquid in a Tank

A rigid tank contains 50 kg of saturated liquid water at $90^{\circ} \mathrm{C}$. Determine the pressure in the tank and the volume of the tank.

Solution A rigid tank contains saturated liquid water. The pressure and volume of the tank are to be determined.
Analysis The state of the saturated liquid water is shown on a $T-v$ diagram in Fig. 3-31. Since saturation conditions exist in the tank, the pressure must be the saturation pressure at $90^{\circ} \mathrm{C}$ :

$$
P=P_{\text {sat @ } 90^{\circ} \mathrm{C}}=70.183 \mathrm{kPa}
$$

(Table A-4)
The specific volume of the saturated liquid at $90^{\circ} \mathrm{C}$ is

$$
v=v_{f @ 90^{\circ} \mathrm{C}}=0.001036 \mathrm{~m}^{3} / \mathrm{kg}
$$

(Table A-4)
Then the total volume of the tank becomes

$$
V=m v=(50 \mathrm{~kg})\left(0.001036 \mathrm{~m}^{3} / \mathrm{kg}\right)=0.0518 \mathrm{~m}^{3}
$$

## EXAMPLE 3-2 Temperature of Saturated Vapor in a Cylinder

A piston-cylinder device contains $2 \mathrm{ft}^{3}$ of saturated water vapor at 50-psia pressure. Determine the temperature and the mass of the vapor inside the cylinder.

Solution A cylinder contains saturated water vapor. The temperature and the mass of vapor are to be determined.
Analysis The state of the saturated water vapor is shown on a $P-v$ diagram in Fig. 3-32. Since the cylinder contains saturated vapor at 50 psia, the temperature inside must be the saturation temperature at this pressure:

$$
T=T_{\text {sat } @ 50 \text { psia }}=280.99^{\circ} \mathbf{F} \quad(\text { Table A-5E) }
$$

The specific volume of the saturated vapor at 50 psia is

$$
v=v_{g @ 50 \text { psia }}=8.5175 \mathrm{ft}^{3} / \mathrm{lbm} \quad(\text { Table A-5E })
$$

Then the mass of water vapor inside the cylinder becomes

$$
m=\frac{V}{V}=\frac{2 \mathrm{ft}^{3}}{8.5175 \mathrm{ft}^{3} / \mathrm{lbm}}=0.235 \mathrm{lbm}
$$

## EXAMPLE 3-3 Volume and Energy Change during Evaporation

A mass of 200 g of saturated liquid water is completely vaporized at a constant pressure of 100 kPa . Determine (a) the volume change and (b) the amount of energy transferred to the water.

Solution Saturated liquid water is vaporized at constant pressure. The volume change and the energy transferred are to be determined.
Analysis (a) The process described is illustrated on a P-v diagram in Fig. 3-33. The volume change per unit mass during a vaporization process is $v_{f g}$, which
is the difference between $v_{g}$ and $v_{f}$. Reading these values from Table A-5 at 100 kPa and substituting yield

$$
v_{f g}=v_{g}-v_{f}=1.6941-0.001043=1.6931 \mathrm{~m}^{3} / \mathrm{kg}
$$

Thus,

$$
\Delta V=m V_{f g}=(0.2 \mathrm{~kg})\left(1.6931 \mathrm{~m}^{3} / \mathrm{kg}\right)=0.3386 \mathrm{~m}^{3}
$$

(b) The amount of energy needed to vaporize a unit mass of a substance at a given pressure is the enthalpy of vaporization at that pressure, which is $h_{f g}=$ $2257.5 \mathrm{~kJ} / \mathrm{kg}$ for water at 100 kPa . Thus, the amount of energy transferred is

$$
m h_{f g}=(0.2 \mathrm{~kg})(2257.5 \mathrm{~kJ} / \mathrm{kg})=451.5 \mathrm{~kJ}
$$

Discussion Note that we have considered the first four decimal digits of $v_{f g}$ and disregarded the rest. This is because $v_{g}$ has significant numbers to the first four decimal places only, and we do not know the numbers in the other decimal places. Copying all the digits from the calculator would mean that we are assuming $v_{g}=1.694100$, which is not necessarily the case. It could very well be that $v_{g}=1.694138$ since this number, too, would truncate to 1.6941. All the digits in our result (1.6931) are significant. But if we did not truncate the result, we would obtain $v_{f g}=1.693057$, which falsely implies that our result is accurate to the sixth decimal place.

## 1b Saturated Liquid-Vapor Mixture

During a vaporization process, a substance exists as part liquid and part vapor. That is, it is a mixture of saturated liquid and saturated vapor (Fig. 3-34). To analyze this mixture properly, we need to know the proportions of the liquid and vapor phases in the mixture. This is done by defining a new property called the quality $x$ as the ratio of the mass of vapor to the total mass of the mixture:

$$
\begin{equation*}
x=\frac{m_{\mathrm{vapor}}}{m_{\mathrm{total}}} \tag{3-3}
\end{equation*}
$$

where

$$
m_{\text {total }}=m_{\text {liquid }}+m_{\text {vapor }}=m_{f}+m_{g}
$$

Quality has significance for saturated mixtures only. It has no meaning in the compressed liquid or superheated vapor regions. Its value is between 0 and 1. The quality of a system that consists of saturated liquid is 0 (or 0 percent), and the quality of a system consisting of saturated vapor is 1 (or 100 percent). In saturated mixtures, quality can serve as one of the two independent intensive properties needed to describe a state. Note that the properties of the saturated liquid are the same whether it exists alone or in a mixture with saturated vapor. During the vaporization process, only the amount of saturated liquid changes, not its properties. The same can be said about a saturated vapor.

A saturated mixture can be treated as a combination of two subsystems: the saturated liquid and the saturated vapor. However, the amount of mass for each phase is usually not known. Therefore, it is often more convenient


FIGURE 3-33
Schematic and $P-\vee$ diagram for Example 3-3.


FIGURE 3-34
The relative amounts of liquid and vapor phases in a saturated mixture are specified by the quality $x$.


FIGURE 3-35
A two-phase system can be treated as a homogeneous mixture for convenience.


FIGURE 3-36
Quality is related to the horizontal distances on $P-\vee$ and $T-\vee$ diagrams.
to imagine that the two phases are mixed well, forming a homogeneous mixture (Fig. 3-35). Then the properties of this "mixture" will simply be the average properties of the saturated liquid-vapor mixture under consideration. Here is how it is done.

Consider a tank that contains a saturated liquid-vapor mixture. The volume occupied by saturated liquid is $V_{f}$, and the volume occupied by saturated vapor is $V_{g}$. The total volume $V$ is the sum of the two:

$$
\begin{aligned}
V & =V_{f}+V_{g} \\
V=m \vee \longrightarrow m_{t} v_{\text {avg }} & =m_{f} V_{f}+m_{g} V_{g} \\
m_{f}=m_{t}-m_{g} \longrightarrow m_{t} V_{\mathrm{avg}} & =\left(m_{t}-m_{g}\right) V_{f}+m_{g} v_{g}
\end{aligned}
$$

Dividing by $m_{t}$ yields

$$
v_{\text {avg }}=(1-x) v_{f}+x v_{g}
$$

since $x=m_{g} / m_{t}$. This relation can also be expressed as

$$
\begin{equation*}
v_{\text {avg }}=v_{f}+x v_{f g} \quad\left(\mathrm{~m}^{3} / \mathrm{kg}\right) \tag{3-4}
\end{equation*}
$$

where $v_{f g}=v_{g}-v_{f}$. Solving for quality, we obtain

$$
\begin{equation*}
x=\frac{V_{\mathrm{avg}}-V_{f}}{V_{f g}} \tag{3-5}
\end{equation*}
$$

Based on this equation, quality can be related to the horizontal distances on a $P-\vee$ or $T-\vee$ diagram (Fig. 3-36). At a given temperature or pressure, the numerator of Eq. 3-5 is the distance between the actual state and the saturated liquid state, and the denominator is the length of the entire horizontal line that connects the saturated liquid and saturated vapor states. A state of 50 percent quality lies in the middle of this horizontal line.
The analysis given above can be repeated for internal energy and enthalpy with the following results:

$$
\begin{array}{ll}
u_{\mathrm{avg}}=u_{f}+x u_{f g} & (\mathrm{~kJ} / \mathrm{kg}) \\
h_{\mathrm{avg}}=h_{f}+x h_{f g} & (\mathrm{~kJ} / \mathrm{kg}) \tag{3-7}
\end{array}
$$

All the results are of the same format, and they can be summarized in a single equation as

$$
y_{\text {avg }}=y_{f}+x y_{f g}
$$

where $y$ is $v, u$, or $h$. The subscript "avg" (for "average") is usually dropped for simplicity. The values of the average properties of the mixtures are always between the values of the saturated liquid and the saturated vapor properties (Fig. 3-37). That is,

$$
y_{f} \leq y_{\text {avg }} \leq y_{g}
$$

Finally, all the saturated-mixture states are located under the saturation curve, and to analyze saturated mixtures, all we need are saturated liquid and saturated vapor data (Tables A-4 and A-5 in the case of water).

## EXAMPLE 3-4 Pressure and Volume of a Saturated Mixture

A rigid tank contains 10 kg of water at $90^{\circ} \mathrm{C}$. If 8 kg of the water is in the liquid form and the rest is in the vapor form, determine (a) the pressure in the tank and $(b)$ the volume of the tank.

Solution A rigid tank contains saturated mixture. The pressure and the volume of the tank are to be determined.
Analysis (a) The state of the saturated liquid-vapor mixture is shown in Fig. 3-38. Since the two phases coexist in equilibrium, we have a saturated mixture, and the pressure must be the saturation pressure at the given temperature:

$$
P=P_{\text {sat @ } 90^{\circ} \mathrm{C}}=70.183 \mathrm{kPa} \quad(\text { Table A-4) }
$$

(b) At $90^{\circ} \mathrm{C}$, we have $v_{f}=0.001036 \mathrm{~m}^{3} / \mathrm{kg}$ and $v_{g}=2.3593 \mathrm{~m}^{3} / \mathrm{kg}$ (Table A-4). One way of finding the volume of the tank is to determine the volume occupied by each phase and then add them:

$$
\begin{aligned}
V & =V_{f}+V_{g}=m_{f} V_{f}+m_{g} V_{g} \\
& =(8 \mathrm{~kg})\left(0.001036 \mathrm{~m}^{3} / \mathrm{kg}\right)+(2 \mathrm{~kg})\left(2.3593 \mathrm{~m}^{3} / \mathrm{kg}\right) \\
& =4.73 \mathrm{~m}^{3}
\end{aligned}
$$

Another way is to first determine the quality $x$, then the average specific volume $v$, and finally the total volume:

$$
\begin{aligned}
x & =\frac{m_{g}}{m_{t}}=\frac{2 \mathrm{~kg}}{10 \mathrm{~kg}}=0.2 \\
v & =v_{f}+x v_{f g} \\
& =0.001036 \mathrm{~m}^{3} / \mathrm{kg}+(0.2)\left[(2.3593-0.001036) \mathrm{m}^{3} / \mathrm{kg}\right] \\
& =0.473 \mathrm{~m}^{3} / \mathrm{kg}
\end{aligned}
$$

and

$$
V=m v=(10 \mathrm{~kg})\left(0.473 \mathrm{~m}^{3} / \mathrm{kg}\right)=4.73 \mathrm{~m}^{3}
$$

Discussion The first method appears to be easier in this case since the masses of each phase are given. In most cases, however, the masses of each phase are not available, and the second method becomes more convenient.

## EXAMPLE 3-5 Properties of Saturated Liquid-Vapor Mixture

An 80-L vessel contains 4 kg of refrigerant-134a at a pressure of 160 kPa . Determine (a) the temperature, (b) the quality, (c) the enthalpy of the refrigerant, and (d) the volume occupied by the vapor phase.

Solution A vessel is filled with refrigerant-134a. Some properties of the refrigerant are to be determined.
Analysis (a) The state of the saturated liquid-vapor mixture is shown in Fig. 3-39. At this point we do not know whether the refrigerant is in the compressed liquid, superheated vapor, or saturated mixture region. This can


FIGURE 3-37
The $v$ value of a saturated liquid-vapor mixture lies between the $V_{f}$ and $V_{g}$ values at the specified $T$ or $P$.


FIGURE 3-38
Schematic and $T-\vee$ diagram for Example 3-4.

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FIGURE 3-39
Schematic and $P-\vee$ diagram for Example 3-5.


FIGURE 3-40
A partial listing of Table A-6.
be determined by comparing a suitable property to the saturated liquid and saturated vapor values. From the information given, we can determine the specific volume:

$$
v=\frac{V}{m}=\frac{0.080 \mathrm{~m}^{3}}{4 \mathrm{~kg}}=0.02 \mathrm{~m}^{3} / \mathrm{kg}
$$

At 160 kPa , we read

$$
\begin{aligned}
& v_{f}=0.0007437 \mathrm{~m}^{3} / \mathrm{kg} \\
& v_{g}=0.12348 \mathrm{~m}^{3} / \mathrm{kg}
\end{aligned}
$$

(Table A-12)
Obviously, $v_{f}<v<v_{g}$, and, the refrigerant is in the saturated mixture region. Thus, the temperature must be the saturation temperature at the specified pressure:

$$
T=T_{\text {sat @ } @ 160 \mathrm{kPa}}=-15.60^{\circ} \mathrm{C}
$$

(b) Quality can be determined from

$$
x=\frac{v-v_{f}}{v_{f g}}=\frac{0.02-0.0007437}{0.12348-0.0007437}=\mathbf{0 . 1 5 7}
$$

(c) At 160 kPa , we also read from Table A-12 that $h_{f}=31.21 \mathrm{~kJ} / \mathrm{kg}$ and $h_{f g}=$ $209.90 \mathrm{~kJ} / \mathrm{kg}$. Then,

$$
\begin{aligned}
h & =h_{f}+x h_{f g} \\
& =31.21 \mathrm{~kJ} / \mathrm{kg}+(0.157)(209.90 \mathrm{~kJ} / \mathrm{kg}) \\
& =\mathbf{6 4 . 2} \mathbf{~ k J} / \mathbf{k g}
\end{aligned}
$$

(d) The mass of the vapor is

$$
m_{g}=x m_{t}=(0.157)(4 \mathrm{~kg})=0.628 \mathrm{~kg}
$$

and the volume occupied by the vapor phase is

$$
V_{g}=m_{g} \vee_{g}=(0.628 \mathrm{~kg})\left(0.12348 \mathrm{~m}^{3} / \mathrm{kg}\right)=0.0775 \mathrm{~m}^{3}(\text { or } 77.5 \mathrm{~L})
$$

The rest of the volume ( 2.5 L ) is occupied by the liquid.

Property tables are also available for saturated solid-vapor mixtures. Properties of saturated ice-water vapor mixtures, for example, are listed in Table A-8. Saturated solid-vapor mixtures can be handled just as saturated liquid-vapor mixtures.

## 2 Superheated Vapor

In the region to the right of the saturated vapor line and at temperatures above the critical point temperature, a substance exists as superheated vapor. Since the superheated region is a single-phase region (vapor phase only), temperature and pressure are no longer dependent properties and they can conveniently be used as the two independent properties in the tables. The format of the superheated vapor tables is illustrated in Fig. 3-40.

In these tables, the properties are listed against temperature for selected pressures starting with the saturated vapor data. The saturation temperature is given in parentheses following the pressure value.

Compared to saturated vapor, superheated vapor is characterized by
Lower pressures $\left(P<P_{\text {sat }}\right.$ at a given $\left.T\right)$
Higher tempreatures $\left(T>T_{\text {sat }}\right.$ at a given $\left.P\right)$
Higher specific volumes $\left(v>v_{g}\right.$ at a given $P$ or $\left.T\right)$
Higher internal energies $\left(u>u_{g}\right.$ at a given $P$ or $\left.T\right)$
Higher enthalpies $\left(h>h_{g}\right.$ at a given $P$ or $\left.T\right)$

## EXAMPLE 3-6 Internal Energy of Superheated Vapor

Determine the internal energy of water at 20 psia and $400^{\circ} \mathrm{F}$.
Solution The internal energy of water at a specified state is to be determined.
Analysis At 20 psia, the saturation temperature is $227.92^{\circ}$. Since $T>$ $T_{\text {sat }}$, the water is in the superheated vapor region. Then the internal energy at the given temperature and pressure is determined from the superheated vapor table (Table A-6E) to be

$$
u=1145.1 \mathrm{Btu} / \mathrm{lbm}
$$

## EXAMPLE 3-7 Temperature of Superheated Vapor

Determine the temperature of water at a state of $P=0.5 \mathrm{MPa}$ and $h=$ $2890 \mathrm{~kJ} / \mathrm{kg}$.

Solution The temperature of water at a specified state is to be determined. Analysis At 0.5 MPa, the enthalpy of saturated water vapor is $h_{g}=2748.1$ $\mathrm{kJ} / \mathrm{kg}$. Since $h>h_{g}$, as shown in Fig. 3-41, we again have superheated vapor. Under 0.5 MPa in Table A-6 we read

| $T,{ }^{\circ} \mathrm{C}$ | $h, \mathrm{~kJ} / \mathrm{kg}$ |
| :--- | :--- |
| 200 | 2855.8 |
| 250 | 2961.0 |

Obviously, the temperature is between 200 and $250^{\circ} \mathrm{C}$. By linear interpolation it is determined to be

$$
T=216.3^{\circ} \mathrm{C}
$$

## 3 Compressed Liquid

Compressed liquid tables are not as commonly available, and Table A-7 is the only compressed liquid table in this text. The format of Table A-7 is very much like the format of the superheated vapor tables. One reason for the lack of compressed liquid data is the relative independence of compressed liquid properties from pressure. Variation of properties of compressed liquid with pressure is very mild. Increasing the pressure 100 times often causes properties to change less than 1 percent.


FIGURE 3-41
At a specified $P$, superheated vapor exists at a higher $h$ than the saturated vapor (Example 3-7).

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FIGURE 3-42
A compressed liquid may be approximated as a saturated liquid at the given temperature.


FIGURE 3-43
Schematic and $T-u$ diagram for Example 3-8.

In the absence of compressed liquid data, a general approximation is to treat compressed liquid as saturated liquid at the given temperature (Fig. 3-42). This is because the compressed liquid properties depend on temperature much more strongly than they do on pressure. Thus,

$$
\begin{equation*}
y \cong y_{f @ T} \tag{3-8}
\end{equation*}
$$

for compressed liquids, where $y$ is $v, u$, or $h$. Of these three properties, the property whose value is most sensitive to variations in the pressure is the enthalpy $h$. Although the above approximation results in negligible error in $v$ and $u$, the error in $h$ may reach undesirable levels. However, the error in $h$ at low to moderate pressures and temperatures can be reduced significantly by evaluating it from

$$
\begin{equation*}
h \cong h_{f @ T}+V_{f @ T}\left(P-P_{\text {sat @T }}\right) \tag{3-9}
\end{equation*}
$$

instead of taking it to be just $h_{f}$. Note, however, that the approximation in Eq. 3-9 does not yield any significant improvement at moderate to high temperatures and pressures, and it may even backfire and result in greater error due to overcorrection at very high temperatures and pressures (see Kostic, Ref. 4).

In general, a compressed liquid is characterized by
Higher pressures $\left(P>P_{\text {sat }}\right.$ at a given $\left.T\right)$
Lower tempreatures $\left(T<T_{\text {sat }}\right.$ at a given $\left.P\right)$
Lower specific volumes $\left(v<v_{f}\right.$ at a given $P$ or $\left.T\right)$
Lower internal energies ( $u<u_{f}$ at a given $P$ or $T$ )
Lower enthalpies $\left(h<h_{f}\right.$ at a given $P$ or $\left.T\right)$
But unlike superheated vapor, the compressed liquid properties are not much different from the corresponding saturated liquid values.

## EXAMPLE 3-8 Approximating Compressed Liquid as Saturated Liquid

Determine the internal energy of compressed liquid water at $80^{\circ} \mathrm{C}$ and 5 MPa , using (a) data from the compressed liquid table and (b) saturated liquid data. What is the error involved in the second case?

Solution The exact and approximate values of the internal energy of liquid water are to be determined.
Analysis At $80^{\circ} \mathrm{C}$, the saturation pressure of water is 47.416 kPa , and since $5 \mathrm{MPa}>P_{\text {sat }}$, we obviously have compressed liquid, as shown in Fig. 3-43.
(a) From the compressed liquid table (Table A-7)

$$
\left.\begin{array}{l}
P=5 \mathrm{MPa} \\
T=80^{\circ} \mathrm{C}
\end{array}\right\} u=333.82 \mathrm{~kJ} / \mathrm{kg}
$$

(b) From the saturation table (Table A-4), we read

$$
u \cong u_{f @ 80^{\circ} \mathrm{C}}=334.97 \mathrm{~kJ} / \mathbf{k g}
$$

The error involved is

$$
\frac{334.97-333.82}{333.82} \times 100=0.34 \%
$$

which is less than 1 percent.

## Reference State and Reference Values

The values of $u, h$, and $s$ cannot be measured directly, and they are calculated from measurable properties using the relations between thermodynamic properties. However, those relations give the changes in properties, not the values of properties at specified states. Therefore, we need to choose a convenient reference state and assign a value of zero for a convenient property or properties at that state. For water, the state of saturated liquid at $0.01^{\circ} \mathrm{C}$ is taken as the reference state, and the internal energy and entropy are assigned zero values at that state. For refrigerant-134a, the state of saturated liquid at $-40^{\circ} \mathrm{C}$ is taken as the reference state, and the enthalpy and entropy are assigned zero values at that state. Note that some properties may have negative values as a result of the reference state chosen.

It should be mentioned that sometimes different tables list different values for some properties at the same state as a result of using a different reference state. However, in thermodynamics we are concerned with the changes in properties, and the reference state chosen is of no consequence in calculations as long as we use values from a single consistent set of tables or charts.

## EXAMPLE 3-9 The Use of Steam Tables to Determine Properties

Determine the missing properties and the phase descriptions in the following table for water:

|  | $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $u, \mathrm{~kJ} / \mathrm{kg}$ | $x$ | Phase description |
| :--- | ---: | ---: | ---: | :---: | :---: |
| $(a)$ |  | 200 |  | 0.6 |  |
| (b) | 125 |  | 1600 |  |  |
| (c) |  | 1000 | 2950 |  |  |
| (d) | 75 | 500 |  |  |  |
| (e) |  | 850 |  | 0.0 |  |

Solution Properties and phase descriptions of water are to be determined at various states.
Analysis (a) The quality is given to be $x=0.6$, which implies that 60 percent of the mass is in the vapor phase and the remaining 40 percent is in the liquid phase. Therefore, we have saturated liquid-vapor mixture at a pressure of 200 kPa . Then the temperature must be the saturation temperature at the given pressure:

$$
T=T_{\text {sat } @ 200 \mathrm{kPa}}=120.21^{\circ} \mathrm{C} \quad(\text { Table A-5 })
$$

At 200 kPa , we also read from Table A-5 that $u_{f}=504.50 \mathrm{~kJ} / \mathrm{kg}$ and $u_{f g}=$ $2024.6 \mathrm{~kJ} / \mathrm{kg}$. Then the average internal energy of the mixture is

$$
\begin{aligned}
u & =u_{f}+x u_{f g} \\
& =504.50 \mathrm{~kJ} / \mathrm{kg}+(0.6)(2024.6 \mathrm{~kJ} / \mathrm{kg}) \\
& =\mathbf{1 7 1 9 . 2 6} \mathbf{~ k J} / \mathbf{k g}
\end{aligned}
$$

(b) This time the temperature and the internal energy are given, but we do not know which table to use to determine the missing properties because we have no clue as to whether we have saturated mixture, compressed liquid, or superheated vapor. To determine the region we are in, we first go to the


FIGURE 3-44
At a given $P$ and $T$, a pure substance will exist as a compressed liquid if $T<T_{\text {sat } @ P}$.
saturation table (Table A-4) and determine the $u_{f}$ and $u_{g}$ values at the given temperature. At $125^{\circ} \mathrm{C}$, we read $u_{f}=524.83 \mathrm{~kJ} / \mathrm{kg}$ and $u_{g}=2534.3 \mathrm{~kJ} / \mathrm{kg}$. Next we compare the given $u$ value to these $u_{f}$ and $u_{g}$ values, keeping in mind that

$$
\begin{array}{lll}
\text { if } & u<u_{f} & \text { we have compressed liquid } \\
\text { if } & u_{f} \leq u \leq u_{g} & \text { we have saturated mixture } \\
\text { if } & u>u_{g} & \text { we have superheated vapor }
\end{array}
$$

In our case the given $u$ value is 1600 , which falls between the $u_{f}$ and $u_{g}$ values at $125^{\circ} \mathrm{C}$. Therefore, we have saturated liquid-vapor mixture. Then the pressure must be the saturation pressure at the given temperature:

$$
P=P_{\text {sat } @ 125^{\circ} \mathrm{C}}=\mathbf{2 3 2 . 2 3} \mathbf{~ k P a} \quad(\text { Table A-4) }
$$

The quality is determined from

$$
x=\frac{u-u_{f}}{u_{f g}}=\frac{1600-524.83}{2009.5}=0.535
$$

The criteria above for determining whether we have compressed liquid, saturated mixture, or superheated vapor can also be used when enthalpy $h$ or specific volume $v$ is given instead of internal energy $u$, or when pressure is given instead of temperature.
(c) This is similar to case (b), except pressure is given instead of temperature. Following the argument given above, we read the $u_{f}$ and $u_{g}$ values at the specified pressure. At 1 MPa , we have $u_{f}=761.39 \mathrm{~kJ} / \mathrm{kg}$ and $u_{g}=2582.8$ $\mathrm{kJ} / \mathrm{kg}$. The specified $u$ value is $2950 \mathrm{~kJ} / \mathrm{kg}$, which is greater than the $u_{g}$ value at 1 MPa . Therefore, we have superheated vapor, and the temperature at this state is determined from the superheated vapor table by interpolation to be

$$
T=395.2^{\circ} \mathrm{C} \quad(\text { Table A-6) }
$$

We would leave the quality column blank in this case since quality has no meaning for a superheated vapor.
(d) In this case the temperature and pressure are given, but again we cannot tell which table to use to determine the missing properties because we do not know whether we have saturated mixture, compressed liquid, or superheated vapor. To determine the region we are in, we go to the saturation table (Table A-5) and determine the saturation temperature value at the given pressure. At 500 kPa , we have $T_{\text {sat }}=151.83^{\circ} \mathrm{C}$. We then compare the given $T$ value to this $T_{\text {sat }}$ value, keeping in mind that

$$
\begin{array}{lll}
\text { if } & T<T_{\text {sat @ given } P} & \text { we have compressed liquid } \\
\text { if } & T=T_{\text {sat @ given } P} & \text { we have saturated mixture } \\
\text { if } & T>T_{\text {sat @ given } P} & \text { we have superheated vapor }
\end{array}
$$

In our case, the given $T$ value is $75^{\circ} \mathrm{C}$, which is less than the $T_{\text {sat }}$ value at the specified pressure. Therefore, we have compressed liquid (Fig. 3-44), and normally we would determine the internal energy value from the compressed liquid table. But in this case the given pressure is much lower than the lowest pressure value in the compressed liquid table (which is 5 MPa ), and therefore we are justified to treat the compressed liquid as saturated liquid at the given temperature (not pressure):

$$
u \cong u_{f @ 75^{\circ} \mathrm{C}}=313.99 \mathrm{~kJ} / \mathbf{k g} \quad(\text { Table A-4) }
$$

We would leave the quality column blank in this case since quality has no meaning in the compressed liquid region.
(e) The quality is given to be $x=0$, and thus we have saturated liquid at the specified pressure of 850 kPa . Then the temperature must be the saturation temperature at the given pressure, and the internal energy must have the saturated liquid value:

$$
\begin{aligned}
& T=T_{\text {sat @ } 850 \mathrm{kPa}}=\mathbf{1 7 2 . 9 4}^{\circ} \mathrm{C} \\
& u=u_{f @ 850 \mathrm{kPa}}=731.00 \mathrm{~kJ} / \mathbf{k g}
\end{aligned}
$$

(Table A-5)

## 3-6 - THE IDEAL-GAS EQUATION OF STATE

Property tables provide very accurate information about the properties, but they are bulky and vulnerable to typographical errors. A more practical and desirable approach would be to have some simple relations among the properties that are sufficiently general and accurate.

Any equation that relates the pressure, temperature, and specific volume of a substance is called an equation of state. Property relations that involve other properties of a substance at equilibrium states are also referred to as equations of state. There are several equations of state, some simple and others very complex. The simplest and best-known equation of state for substances in the gas phase is the ideal-gas equation of state. This equation predicts the $P-\vee-T$ behavior of a gas quite accurately within some properly selected region.

Gas and vapor are often used as synonymous words. The vapor phase of a substance is customarily called a gas when it is above the critical temperature. Vapor usually implies a gas that is not far from a state of condensation.

In 1662, Robert Boyle, an Englishman, observed during his experiments with a vacuum chamber that the pressure of gases is inversely proportional to their volume. In 1802, J. Charles and J. Gay-Lussac, Frenchmen, experimentally determined that at low pressures the volume of a gas is proportional to its temperature. That is,

$$
P=R\left(\frac{T}{V}\right)
$$

or

$$
\begin{equation*}
P \vee=R T \tag{3-10}
\end{equation*}
$$

where the constant of proportionality $R$ is called the gas constant. Equation $3-10$ is called the ideal-gas equation of state, or simply the ideal-gas relation, and a gas that obeys this relation is called an ideal gas. In this equation, $P$ is the absolute pressure, $T$ is the absolute temperature, and $v$ is the specific volume.

The gas constant $R$ is different for each gas (Fig. 3-45) and is determined from

$$
R=\frac{R_{u}}{M} \quad\left(\mathrm{~kJ} / \mathrm{kg} \cdot \mathrm{~K} \text { or } \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} \cdot \mathrm{~K}\right)
$$

where $R_{u}$ is the universal gas constant and $M$ is the molar mass (also


FIGURE 3-45
Different substances have different gas constants.

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FIGURE 3-46
Properties per unit mole are denoted with a bar on the top.


FIGURE 3-47
The ideal-gas relation often is not applicable to real gases; thus, care should be exercised when using it.

[^1]called molecular weight) of the gas. The constant $R_{u}$ is the same for all substances, and its value is
\[

R_{u}=\left\{$$
\begin{array}{l}
8.31447 \mathrm{~kJ} / \mathrm{kmol} \cdot \mathrm{~K}  \tag{3-11}\\
8.31447 \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kmol} \cdot \mathrm{~K} \\
0.0831447 \mathrm{bar} \cdot \mathrm{~m}^{3} / \mathrm{kmol} \cdot \mathrm{~K} \\
1.98588 \mathrm{Btu} / \mathrm{lbmol} \cdot \mathrm{R} \\
10.7316 \mathrm{psia} \cdot \mathrm{ft}^{3} / \mathrm{lbmol} \cdot \mathrm{R} \\
1545.37 \mathrm{ft} \cdot \mathrm{lbf} / \mathrm{lbmol} \cdot \mathrm{R}
\end{array}
$$\right.
\]

The molar mass $M$ can simply be defined as the mass of one mole (also called a gram-mole, abbreviated gmol) of a substance in grams, or the mass of one kmol (also called a kilogram-mole, abbreviated kgmol) in kilograms. In English units, it is the mass of 1 lbmol in lbm . Notice that the molar mass of a substance has the same numerical value in both unit systems because of the way it is defined. When we say the molar mass of nitrogen is 28, it simply means the mass of 1 kmol of nitrogen is 28 kg , or the mass of 1 lbmol of nitrogen is 28 lbm . That is, $M=28 \mathrm{~kg} / \mathrm{kmol}=28 \mathrm{lbm} / \mathrm{lbmol}$. The mass of a system is equal to the product of its molar mass $M$ and the mole number $N$ :

$$
\begin{equation*}
m=M N \quad(\mathrm{~kg}) \tag{3-12}
\end{equation*}
$$

The values of $R$ and $M$ for several substances are given in Table A-1.
The ideal-gas equation of state can be written in several different forms:

$$
\begin{array}{r}
V=m \vee \longrightarrow P V=m R T \\
m R=(M N) R=N R_{u} \longrightarrow P V=N R_{u} T \\
V=N \bar{V} \longrightarrow P \bar{V}=R_{u} T \tag{3-15}
\end{array}
$$

where $\bar{V}$ is the molar specific volume, that is, the volume per unit mole (in $\mathrm{m}^{3} / \mathrm{kmol}$ or $\mathrm{ft}^{3} / \mathrm{lbmol}$ ). A bar above a property denotes values on a unit-mole basis throughout this text (Fig. 3-46).

By writing Eq. 3-13 twice for a fixed mass and simplifying, the properties of an ideal gas at two different states are related to each other by

$$
\begin{equation*}
\frac{P_{1} \vee_{1}}{T_{1}}=\frac{P_{2} \vee_{2}}{T_{2}} \tag{3-16}
\end{equation*}
$$

An ideal gas is an imaginary substance that obeys the relation $P \vee=R T$ (Fig. 3-47). It has been experimentally observed that the ideal-gas relation given closely approximates the $P-\vee-T$ behavior of real gases at low densities. At low pressures and high temperatures, the density of a gas decreases, and the gas behaves as an ideal gas under these conditions. What constitutes low pressure and high temperature is explained later.
In the range of practical interest, many familiar gases such as air, nitrogen, oxygen, hydrogen, helium, argon, neon, krypton, and even heavier gases such as carbon dioxide can be treated as ideal gases with negligible error (often less than 1 percent). Dense gases such as water vapor in steam power plants and refrigerant vapor in refrigerators, however, should not be treated as ideal gases. Instead, the property tables should be used for these substances.

## EXAMPLE 3-10 Mass of Air in a Room

Determine the mass of the air in a room whose dimensions are $4 \mathrm{~m} \times 5 \mathrm{~m} \times$ 6 m at 100 kPa and $25^{\circ} \mathrm{C}$.

Solution The mass of air in a room is to be determined.
Analysis A sketch of the room is given in Fig. 3-48. Air at specified conditions can be treated as an ideal gas. From Table A-1, the gas constant of air is $R=0.287 \mathrm{kPa} \cdot \mathrm{m}^{3} / \mathrm{kg} \cdot \mathrm{K}$, and the absolute temperature is $T=25^{\circ} \mathrm{C}+$ $273=298 \mathrm{~K}$. The volume of the room is

$$
V=(4 \mathrm{~m})(5 \mathrm{~m})(6 \mathrm{~m})=120 \mathrm{~m}^{3}
$$

The mass of air in the room is determined from the ideal-gas relation to be

$$
m=\frac{P V}{R T}=\frac{(100 \mathrm{kPa})\left(120 \mathrm{~m}^{3}\right)}{\left(0.287 \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} \cdot \mathrm{~K}\right)(298 \mathrm{~K})}=\mathbf{1 4 0 . 3} \mathbf{k g}
$$

## Is Water Vapor an Ideal Gas?

This question cannot be answered with a simple yes or no. The error involved in treating water vapor as an ideal gas is calculated and plotted in Fig. 3-49. It is clear from this figure that at pressures below 10 kPa , water vapor can be treated as an ideal gas, regardless of its temperature, with negligible error (less than 0.1 percent). At higher pressures, however, the idealgas assumption yields unacceptable errors, particularly in the vicinity of the critical point and the saturated vapor line (over 100 percent). Therefore, in air-conditioning applications, the water vapor in the air can be treated as an ideal gas with essentially no error since the pressure of the water vapor is very low. In steam power plant applications, however, the pressures involved are usually very high; therefore, ideal-gas relations should not be used.

## 3-7 • COMPRESSIBILITY FACTOR—A MEASURE OF DEVIATION FROM IDEAL-GAS BEHAVIOR

The ideal-gas equation is very simple and thus very convenient to use. However, as illustrated in Fig. 3-49, gases deviate from ideal-gas behavior significantly at states near the saturation region and the critical point. This deviation from ideal-gas behavior at a given temperature and pressure can accurately be accounted for by the introduction of a correction factor called the compressibility factor $Z$ defined as

$$
\begin{equation*}
Z=\frac{P V}{R T} \tag{3-17}
\end{equation*}
$$

or

$$
\begin{equation*}
P v=Z R T \tag{3-18}
\end{equation*}
$$



FIGURE 3-48
Schematic for Example 3-10.

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FIGURE 3-49
Percentage of error
( $\left[\mid V_{\text {table }}-V_{\text {ideal }} / / V_{\text {table }}\right] \times 100$ ) involved in assuming steam to be an ideal gas, and the region where steam can be treated as an ideal gas with less than 1 percent error.


FIGURE 3-50
The compressibility factor is unity for ideal gases.


It can also be expressed as

$$
\begin{equation*}
Z=\frac{V_{\text {actual }}}{V_{\text {ideal }}} \tag{3-19}
\end{equation*}
$$

where $v_{\text {ideal }}=R T / P$. Obviously, $Z=1$ for ideal gases. For real gases $Z$ can be greater than or less than unity (Fig. 3-50). The farther away $Z$ is from unity, the more the gas deviates from ideal-gas behavior.

We have said that gases follow the ideal-gas equation closely at low pressures and high temperatures. But what exactly constitutes low pressure or high temperature? Is $-100^{\circ} \mathrm{C}$ a low temperature? It definitely is for most substances but not for air. Air (or nitrogen) can be treated as an ideal gas at this temperature and atmospheric pressure with an error under 1 percent. This is because nitrogen is well over its critical temperature $\left(-147^{\circ} \mathrm{C}\right)$ and away from the saturation region. At this temperature and pressure, however, most substances would exist in the solid phase. Therefore, the pressure or temperature of a substance is high or low relative to its critical temperature or pressure.

Gases behave differently at a given temperature and pressure, but they behave very much the same at temperatures and pressures normalized with respect to their critical temperatures and pressures. The normalization is done as

$$
\begin{equation*}
P_{R}=\frac{P}{P_{\mathrm{cr}}} \quad \text { and } \quad T_{R}=\frac{T}{T_{\mathrm{cr}}} \tag{3-20}
\end{equation*}
$$

Here $P_{R}$ is called the reduced pressure and $T_{R}$ the reduced temperature. The $Z$ factor for all gases is approximately the same at the same reduced pressure and temperature. This is called the principle of corresponding states. In Fig. 3-51, the experimentally determined $Z$ values are plotted against $P_{R}$ and $T_{R}$ for several gases. The gases seem to obey the principle of corresponding states reasonably well. By curve-fitting all the data, we


FIGURE 3-51
Comparison of $Z$ factors for various gases.
Source: Gour-Jen Su, "Modified Law of Corresponding States," Ind. Eng. Chem. (international ed.) 38 (1946), p. 803.

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FIGURE 3-52
At very low pressures, all gases approach ideal-gas behavior (regardless of their temperature).


FIGURE 3-53
Gases deviate from the ideal-gas behavior the most in the neighborhood of the critical point.
obtain the generalized compressibility chart that can be used for all gases (Fig. A-15).
The following observations can be made from the generalized compressibility chart:

1. At very low pressures $\left(P_{R} \ll 1\right)$, gases behave as an ideal gas regardless of temperature (Fig. 3-52),
2. At high temperatures $\left(T_{R}>2\right)$, ideal-gas behavior can be assumed with good accuracy regardless of pressure (except when $P_{R} \gg 1$ ).
3. The deviation of a gas from ideal-gas behavior is greatest in the vicinity of the critical point (Fig. 3-53).

## EXAMPLE 3-11 The Use of Generalized Charts

Determine the specific volume of refrigerant-134a at 1 MPa and $50^{\circ} \mathrm{C}$, using (a) the ideal-gas equation of state and (b) the generalized compressibility chart. Compare the values obtained to the actual value of $0.021796 \mathrm{~m}^{3} / \mathrm{kg}$ and determine the error involved in each case.

Solution The specific volume of refrigerant-134a is to be determined assuming ideal- and nonideal-gas behavior.
Analysis The gas constant, the critical pressure, and the critical temperature of refrigerant-134a are determined from Table A-1 to be

$$
\begin{aligned}
R & =0.0815 \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} \cdot \mathrm{~K} \\
P_{\mathrm{cr}} & =4.059 \mathrm{MPa} \\
T_{\mathrm{cr}} & =374.2 \mathrm{~K}
\end{aligned}
$$

(a) The specific volume of refrigerant-134a under the ideal-gas assumption is

$$
v=\frac{R T}{P}=\frac{\left(0.0815 \mathrm{kPa} \cdot \mathrm{~m}_{3} / \mathrm{kg} \cdot \mathrm{~K}\right)(323 \mathrm{~K})}{1000 \mathrm{kPa}}=0.026325 \mathrm{~m}^{3} / \mathrm{kg}
$$

Therefore, treating the refrigerant-134a vapor as an ideal gas would result in an error of $(0.026325-0.021796) / 0.021796=0.208$, or 20.8 percent in this case.
(b) To determine the correction factor $Z$ from the compressibility chart, we first need to calculate the reduced pressure and temperature:

$$
\left.\begin{array}{l}
P_{R}=\frac{P}{P_{\mathrm{cr}}}=\frac{1 \mathrm{MPa}}{4.059 \mathrm{MPa}}=0.246 \\
T_{R}=\frac{T}{T_{\mathrm{cr}}}=\frac{323 \mathrm{~K}}{374.2 \mathrm{~K}}=0.863
\end{array}\right\} \quad Z=0.84
$$

Thus

$$
v=Z v_{\text {ideal }}=(0.84)\left(0.026325 \mathrm{~m}^{3} / \mathrm{kg}\right)=\mathbf{0 . 0 2 2 1 1 3} \mathrm{m}^{3} / \mathbf{k g}
$$

Discussion The error in this result is less than 2 percent. Therefore, in the absence of tabulated data, the generalized compressibility chart can be used with confidence.

When $P$ and V , or $T$ and V , are given instead of $P$ and $T$, the generalized compressibility chart can still be used to determine the third property, but it would involve tedious trial and error. Therefore, it is necessary to define one more reduced property called the pseudo-reduced specific volume $v_{R}$ as

$$
\begin{equation*}
V_{R}=\frac{V_{\text {actual }}}{R T_{\mathrm{cr}} / P_{\mathrm{cr}}} \tag{3-21}
\end{equation*}
$$

Note that $\vee_{R}$ is defined differently from $P_{R}$ and $T_{R}$. It is related to $T_{\text {cr }}$ and $P_{\text {cr }}$ instead of $V_{\text {cr }}$. Lines of constant $V_{R}$ are also added to the compressibility charts, and this enables one to determine $T$ or $P$ without having to resort to time-consuming iterations (Fig. 3-54).

## EXAMPLE 3-12

## Using Generalized Charts to Determine Pressure

Determine the pressure of water vapor at $600^{\circ} \mathrm{F}$ and $0.51431 \mathrm{ft}^{3} / \mathrm{lbm}$, using (a) the steam tables, (b) the ideal-gas equation, and (c) the generalized compressibility chart.

Solution The pressure of water vapor is to be determined in three different ways.
Analysis A sketch of the system is given in Fig. 3-55. The gas constant, the critical pressure, and the critical temperature of steam are determined from Table A-1E to be

$$
\begin{aligned}
R & =0.5956 \mathrm{psia} \cdot \mathrm{ft}^{3} / \mathrm{lbm} \cdot \mathrm{R} \\
P_{\text {cr }} & =3200 \mathrm{psia} \\
T_{\text {cr }} & =1164.8 \mathrm{R}
\end{aligned}
$$

(a) The pressure at the specified state is determined from Table A-6E to be

$$
\left.\begin{array}{l}
V=0.51431 \mathrm{ft}^{3} / \mathrm{lbm} \\
T=600^{\circ} \mathrm{F}
\end{array}\right\} \quad P=\mathbf{1 0 0 0} \text { psia }
$$

This is the experimentally determined value, and thus it is the most accurate.
(b) The pressure of steam under the ideal-gas assumption is determined from the ideal-gas relation to be

$$
P=\frac{R T}{V}=\frac{\left(0.5956 \mathrm{psia} \cdot \mathrm{ft}^{3} / \mathrm{lbm} \cdot \mathrm{R}\right)(1060 \mathrm{R})}{0.51431 \mathrm{ft}^{3} / \mathrm{lbm}}=\mathbf{1 2 2 8} \mathbf{~ p s i a}
$$

Therefore, treating the steam as an ideal gas would result in an error of $(1228-1000) / 1000=0.228$, or 22.8 percent in this case.
(c) To determine the correction factor $Z$ from the compressibility chart (Fig. A-15), we first need to calculate the pseudo-reduced specific volume and the reduced temperature:

$$
\left.\begin{array}{l}
\mathrm{V}_{R}=\frac{\mathrm{v}_{\mathrm{actual}}}{R T_{\mathrm{cr}} / P_{\mathrm{cr}}}=\frac{\left(0.51431 \mathrm{ft}^{3} / \mathrm{lbm}\right)(3200 \mathrm{psia})}{\left(0.5956 \mathrm{psia}^{\mathrm{ft}} / \mathrm{lbm} \cdot \mathrm{R}\right)(1164.8 \mathrm{R})}=2.372 \\
T_{R}=\frac{T}{T_{\mathrm{cr}}}=\frac{1060 \mathrm{R}}{1164.8 \mathrm{R}}=0.91
\end{array}\right\} \quad P_{R}=0.33
$$



FIGURE 3-54
The compressibility factor can also be determined from a knowledge of $P_{R}$ and $V_{R}$.

$$
\begin{aligned}
& \quad \mathrm{H}_{2} \mathrm{O} \\
& T=600^{\circ} \mathrm{F} \\
& V=0.51431 \mathrm{ft}^{3} / \mathrm{lbm} \\
& P=?
\end{aligned}
$$

FIGURE 3-55
Schematic for Example 3-12.

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FIGURE 3-56
Results obtained by using the compressibility chart are usually within a few percent of actual values.


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FIGURE 3-57
Several equations of state have been proposed throughout history.

Thus,

$$
P=P_{R} P_{\mathrm{cr}}=(0.33)(3200 \mathrm{psia})=1056 \text { psia }
$$

Discussion Using the compressibility chart reduced the error from 22.8 to 5.6 percent, which is acceptable for most engineering purposes (Fig. 3-56). A bigger chart, of course, would give better resolution and reduce the reading errors. Notice that we did not have to determine $Z$ in this problem since we could read $P_{R}$ directly from the chart.

## 3-8 • OTHER EQUATIONS OF STATE

The ideal-gas equation of state is very simple, but its range of applicability is limited. It is desirable to have equations of state that represent the $P-V-T$ behavior of substances accurately over a larger region with no limitations. Such equations are naturally more complicated. Several equations have been proposed for this purpose (Fig. 3-57), but we shall discuss only three: the van der Waals equation because it is one of the earliest, the Beattie-Bridgeman equation of state because it is one of the best known and is reasonably accurate, and the Benedict-Webb-Rubin equation because it is one of the more recent and is very accurate.

## Van der Waals Equation of State

The van der Waals equation of state was proposed in 1873, and it has two constants that are determined from the behavior of a substance at the critical point. It is given by

$$
\begin{equation*}
\left(P+\frac{a}{v^{2}}\right)(v-b)=R T \tag{3-22}
\end{equation*}
$$

Van der Waals intended to improve the ideal-gas equation of state by including two of the effects not considered in the ideal-gas model: the intermolecular attraction forces and the volume occupied by the molecules themselves. The term $a / v^{2}$ accounts for the intermolecular forces, and $b$ accounts for the volume occupied by the gas molecules. In a room at atmospheric pressure and temperature, the volume actually occupied by molecules is only about one-thousandth of the volume of the room. As the pressure increases, the volume occupied by the molecules becomes an increasingly significant part of the total volume. Van der Waals proposed to correct this by replacing $v$ in the ideal-gas relation with the quantity $v-b$, where $b$ represents the volume occupied by the gas molecules per unit mass.

The determination of the two constants appearing in this equation is based on the observation that the critical isotherm on a $P-\vee$ diagram has a horizontal inflection point at the critical point (Fig. 3-58). Thus, the first and the second derivatives of $P$ with respect to $v$ at the critical point must be zero. That is,

$$
\left(\frac{\partial P}{\partial V}\right)_{T=T_{\mathrm{cr}}=\text { const }}=0 \quad \text { and } \quad\left(\frac{\partial^{2} P}{\partial V^{2}}\right)_{T=T_{\mathrm{ct}}=\text { const }}=0
$$

By performing the differentiations and eliminating $V_{\text {cr }}$, the constants $a$ and $b$ are determined to be

$$
\begin{equation*}
a=\frac{27 R^{2} T_{\mathrm{cr}}^{2}}{64 P_{\mathrm{cr}}} \quad \text { and } \quad b=\frac{R T_{\mathrm{cr}}}{8 P_{\mathrm{cr}}} \tag{3-23}
\end{equation*}
$$

The constants $a$ and $b$ can be determined for any substance from the criticalpoint data alone (Table $\mathrm{A}-1$ ).

The accuracy of the van der Waals equation of state is often inadequate, but it can be improved by using values of $a$ and $b$ that are based on the actual behavior of the gas over a wider range instead of a single point. Despite its limitations, the van der Waals equation of state has a historical value in that it was one of the first attempts to model the behavior of real gases. The van der Waals equation of state can also be expressed on a unitmole basis by replacing the $v$ in Eq. 3-22 by $\bar{\nabla}$ and the $R$ in Eqs. 3-22 and 3-23 by $R_{u}$.

## Beattie-Bridgeman Equation of State

The Beattie-Bridgeman equation, proposed in 1928, is an equation of state based on five experimentally determined constants. It is expressed as

$$
\begin{equation*}
P=\frac{R_{u} T}{\bar{V}^{2}}\left(1-\frac{c}{\bar{V} T^{3}}\right)(\bar{v}+B)-\frac{A}{\bar{v}^{2}} \tag{3-24}
\end{equation*}
$$

where

$$
\begin{equation*}
A=A_{0}\left(1-\frac{a}{\bar{V}}\right) \quad \text { and } \quad B=B_{0}\left(1-\frac{b}{\bar{V}}\right) \tag{3-25}
\end{equation*}
$$

The constants appearing in the above equation are given in Table 3-4 for various substances. The Beattie-Bridgeman equation is known to be reasonably accurate for densities up to about $0.8 \rho_{\text {cr }}$, where $\rho_{\text {cr }}$ is the density of the substance at the critical point.

## Benedict-Webb-Rubin Equation of State

Benedict, Webb, and Rubin extended the Beattie-Bridgeman equation in 1940 by raising the number of constants to eight. It is expressed as

$$
\begin{equation*}
P=\frac{R_{u} T}{\bar{V}}+\left(B_{0} R_{u} T-A_{0}-\frac{C_{0}}{T^{2}}\right) \frac{1}{\bar{V}^{2}}+\frac{b R_{u} T-a}{\bar{v}^{3}}+\frac{a \alpha}{\bar{v}^{6}}+\frac{c}{\bar{v}^{3} T^{2}}\left(1+\frac{\gamma}{\bar{v}^{2}}\right) e^{-\gamma / \bar{v}^{2}} \tag{3-26}
\end{equation*}
$$

The values of the constants appearing in this equation are given in Table 3-4. This equation can handle substances at densities up to about $2.5 \rho_{\text {cr }}$. In 1962, Strobridge further extended this equation by raising the number of constants to 16 (Fig. 3-59).

## Virial Equation of State

The equation of state of a substance can also be expressed in a series form as

$$
\begin{equation*}
P=\frac{R T}{v}+\frac{a(T)}{v^{2}}+\frac{b(T)}{v^{3}}+\frac{c(T)}{v^{4}}+\frac{d(T)}{v^{5}}+\ldots \tag{3-27}
\end{equation*}
$$



FIGURE 3-58
Critical isotherm of a pure substance has an inflection point at the critical state.

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## TABLE 3-4

Constants that appear in the Beattie-Bridgeman and the Benedict-Webb-Rubin equations of state
(a) When $P$ is in $\mathrm{kPa}, \bar{v}$ is in $\mathrm{m}^{3} / \mathrm{kmol}, T$ is in K , and $R_{u}=8.314 \mathrm{kPa} \cdot \mathrm{m}^{3} / \mathrm{kmol} \cdot \mathrm{K}$, the five constants in the BeattieBridgeman equation are as follows:

| Gas | $A_{0}$ | $a$ | $B_{0}$ | $b$ | $c$ |
| :--- | ---: | ---: | ---: | ---: | :---: |
| Air | 131.8441 | 0.01931 | 0.04611 | -0.001101 | $4.34 \times 10^{4}$ |
| Argon, Ar | 130.7802 | 0.02328 | 0.03931 | 0.0 | $5.99 \times 10^{4}$ |
| Carbon dioxide, $\mathrm{CO}_{2}$ | 507.2836 | 0.07132 | 0.10476 | 0.07235 | $6.60 \times 10^{5}$ |
| Helium, He | 2.1886 | 0.05984 | 0.01400 | 0.0 | 40 |
| Hydrogen, $\mathrm{H}_{2}$ | 2.0117 | -0.00506 | 0.02096 | -0.04359 | 504 |
| Nitrogen, $\mathrm{N}_{2}$ | 136.2315 | 0.02617 | 0.05046 | -0.00691 | $4.20 \times 10^{4}$ |
| Oxygen, $\mathrm{O}_{2}$ | 151.0857 | 0.02562 | 0.04624 | 0.004208 | $4.80 \times 10^{4}$ |

Source: Gordon J. Van Wylen and Richard E. Sonntag, Fundamentals of Classical Thermodynamics, English/SI Version, 3rd ed. (New York: John Wiley \& Sons, 1986), p. 46, table 3.3.
(b) When $P$ is in $\mathrm{kPa}, \bar{v}$ is in $\mathrm{m}^{3} / \mathrm{kmol}, T$ is in K , and $R_{u}=8.314 \mathrm{kPa} \cdot \mathrm{m}^{3} / \mathrm{kmol} \cdot \mathrm{K}$, the eight constants in the Benedict-Webb-Rubin equation are as follows:

| Gas | $a$ | $A_{0}$ | $b$ | $B_{0}$ | $c$ | $C_{0}$ | $\alpha$ | $\gamma$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| n-Butane, | 190.68 | 1021.6 | 0.039998 | 0.12436 | $3.205 \times 10^{7}$ | $1.006 \times 10^{8}$ | $1.101 \times 10^{-3}$ | 0.0340 |
| $\mathrm{C}_{4} \mathrm{H}_{10}$ |  |  |  |  |  |  |  |  |

Source: Kenneth Wark, Thermodynamics, 4th ed. (New York: McGraw-Hill, 1983), p. 815, table A-21M. Originally published in H. W. Cooper and J. C. Goldfrank, Hydrocarbon Processing 46, no. 12 (1967), p. 141.


## FIGURE 3-59

Complex equations of state represent the $P-\mathrm{V}-T$ behavior of gases more accurately over a wider range.

This and similar equations are called the virial equations of state, and the coefficients $a(T), b(T), c(T)$, and so on, that are functions of temperature alone are called virial coefficients. These coefficients can be determined experimentally or theoretically from statistical mechanics. Obviously, as the pressure approaches zero, all the virial coefficients will vanish and the equation will reduce to the ideal-gas equation of state. The $P-V-T$ behavior of a substance can be represented accurately with the virial equation of state over a wider range by including a sufficient number of terms. The equations of state discussed here are applicable to the gas phase of the substances only, and thus should not be used for liquids or liquid-vapor mixtures.

Complex equations represent the $P-\mathrm{V}-T$ behavior of substances reasonably well and are very suitable for digital computer applications. For hand calculations, however, it is suggested that the reader use the property tables or the simpler equations of state for convenience. This is particularly true for specific-volume calculations since all the earlier equations are implicit in $V$ and require a trial-and-error approach. The accuracy of the van der Waals,


FIGURE 3-60
Percentage of error involved in various equations of state for nitrogen $\left(\%\right.$ error $\left.=\left[\left(\left|v_{\text {table }}-v_{\text {equation }}\right|\right) / \nu_{\text {table }}\right] \times 100\right)$.

Beattie-Bridgeman, and Benedict-Webb-Rubin equations of state is illustrated in Fig. 3-60. It is apparent from this figure that the Benedict-WebbRubin equation of state is usually the most accurate.

## EXAMPLE 3-13 Different Methods of Evaluating Gas Pressure

Predict the pressure of nitrogen gas at $T=175 \mathrm{~K}$ and $v=0.00375 \mathrm{~m}^{3} / \mathrm{kg}$ on the basis of (a) the ideal-gas equation of state, (b) the van der Waals equation of state, (c) the Beattie-Bridgeman equation of state, and (d) the Benedict-Webb-Rubin equation of state. Compare the values obtained to the experimentally determined value of $10,000 \mathrm{kPa}$.

Solution The pressure of nitrogen gas is to be determined using four different equations of state.

Properties The gas constant of nitrogen gas is $0.2968 \mathrm{kPa} \cdot \mathrm{m}^{3} / \mathrm{kg} \cdot \mathrm{K}$ (Table A-1).

Analysis (a) Using the ideal-gas equation of state, the pressure is found to be

$$
P=\frac{R T}{V}=\frac{\left(0.2968 \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} \cdot \mathrm{~K}\right)(175 \mathrm{~K})}{0.00375 \mathrm{~m}^{3} / \mathrm{kg}}=\mathbf{1 3 , 8 5 1} \mathbf{~ k P a}
$$

which is in error by 38.5 percent.
(b) The van der Waals constants for nitrogen are determined from Eq. 3-23 to be

$$
\begin{aligned}
& a=0.175 \mathrm{~m}^{6} \cdot \mathrm{kPa} / \mathrm{kg}^{2} \\
& b=0.00138 \mathrm{~m}^{3} / \mathrm{kg}
\end{aligned}
$$

From Eq. 3-22,

$$
P=\frac{R T}{V-b}-\frac{a}{V^{2}}=9471 \mathrm{kPa}
$$

which is in error by 5.3 percent.
(c) The constants in the Beattie-Bridgeman equation are determined from Table 3-4 to be

$$
\begin{aligned}
A & =102.29 \\
B & =0.05378 \\
c & =4.2 \times 10^{4}
\end{aligned}
$$

Also, $\bar{v}=M v=(28.013 \mathrm{~kg} / \mathrm{mol})\left(0.00375 \mathrm{~m}^{3} / \mathrm{kg}\right)=0.10505 \mathrm{~m}^{3} / \mathrm{kmol}$. Substituting these values into Eq. 3-24, we obtain

$$
P=\frac{R_{u} T}{\bar{v}^{2}}\left(1-\frac{c}{\bar{V} T^{3}}\right)(\bar{v}+B)-\frac{A}{\bar{v}^{2}}=\mathbf{1 0}, \mathbf{1 1 0} \mathbf{k P a}
$$

which is in error by 1.1 percent.
(d) The constants in the Benedict-Webb-Rubin equation are determined from Table 3-4 to be

$$
\begin{array}{ll}
a=2.54 & A_{0}=106.73 \\
b=0.002328 & B_{0}=0.04074 \\
c=7.379 \times 10^{4} & C_{0}=8.164 \times 10^{5} \\
\alpha=1.272 \times 10^{-4} & \gamma=0.0053
\end{array}
$$

Substituting these values into Eq. 3-26 gives

$$
\begin{aligned}
P= & \frac{R_{u} T}{\bar{V}}+\left(B_{0} R_{u} T-A_{0}-\frac{C_{0}}{T^{2}}\right) \frac{1}{\bar{v}^{2}}+\frac{b R_{u} T-a}{\bar{v}^{3}} \\
& +\frac{a \alpha}{\bar{V}^{6}}+\frac{c}{\overline{\bar{V}}^{3} T^{2}}\left(1+\frac{\gamma}{\bar{v}^{2}}\right) e^{-\gamma / \bar{v}^{2}} \\
= & \mathbf{1 0 , 0 0 9} \mathbf{~ k P a}
\end{aligned}
$$

which is in error by only 0.09 percent. Thus, the accuracy of the Benedict-Webb-Rubin equation of state is rather impressive in this case.

## TOPIC OF SPECIAL INTEREST*

Vapor Pressure and Phase Equilibrium
The pressure in a gas container is due to the individual molecules striking the wall of the container and exerting a force on it. This force is proportional to the average velocity of the molecules and the number of molecules per unit volume of the container (i.e., molar density). Therefore, the pressure exerted by a gas is a strong function of the density and the temperature of the gas. For a gas mixture, the pressure measured by a sensor such as a transducer is the sum of the pressures exerted by the individual gas species, called the partial pressure. It can be shown (see Chap. 13) that the partial pressure of a gas in a mixture is proportional to the number of moles (or the mole fraction) of that gas.

Atmospheric air can be viewed as a mixture of dry air (air with zero moisture content) and water vapor (also referred to as moisture), and the atmospheric pressure is the sum of the pressure of dry air $P_{a}$ and the pressure of water vapor, called the vapor pressure $P_{v}$ (Fig. 3-61). That is,

$$
\begin{equation*}
P_{\mathrm{atm}}=P_{a}+P_{v} \tag{3-28}
\end{equation*}
$$

(Note that in some applications, the phrase "vapor pressure" is used to indicate saturation pressure.) The vapor pressure constitutes a small fraction (usually under 3 percent) of the atmospheric pressure since air is mostly nitrogen and oxygen, and the water molecules constitute a small fraction (usually under 3 percent) of the total molecules in the air. However, the amount of water vapor in the air has a major impact on thermal comfort and many processes such as drying.

Air can hold a certain amount of moisture only, and the ratio of the actual amount of moisture in the air at a given temperature to the maximum amount air can hold at that temperature is called the relative humidity $\phi$. The relative humidity ranges from 0 for dry air to 100 percent for saturated air (air that cannot hold any more moisture). The vapor pressure of saturated air at a given temperature is equal to the saturation pressure of water at that temperature. For example, the vapor pressure of saturated air at $25^{\circ} \mathrm{C}$ is 3.17 kPa .

The amount of moisture in the air is completely specified by the temperature and the relative humidity, and the vapor pressure is related to relative humidity $\phi$ by

$$
\begin{equation*}
P_{v}=\phi P_{\text {sat @ } T} \tag{3-29}
\end{equation*}
$$

where $P_{\text {sat @ T }}$ is the saturation pressure of water at the specified temperature. For example, the vapor pressure of air at $25^{\circ} \mathrm{C}$ and 60 percent relative humidity is

$$
P_{v}=\phi P_{\text {sat @ } 25^{\circ} \mathrm{C}}=0.6 \times(3.17 \mathrm{kPa})=1.90 \mathrm{kPa}
$$

The desirable range of relative humidity for thermal comfort is 40 to 60 percent.
Note that the amount of moisture air can hold is proportional to the saturation pressure, which increases with temperature. Therefore, air can hold more moisture at higher temperatures. Dropping the temperature of moist air reduces its moisture capacity and may result in the condensation of some of the moisture in the air as suspended water droplets (fog) or as a liquid film on cold surfaces (dew). So it is no surprise that fog and dew are common occurrences at humid locations especially in the early morning hours when

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(a) Before

(b) After

FIGURE 3-62
Whenever there is a concentration difference of a physical quantity in a medium, nature tends to equalize things by forcing a flow from the high to the low concentration region.


FIGURE 3-63
When open to the atmosphere, water is in phase equilibrium with the vapor in the air if the vapor pressure is equal to the saturation pressure of water.
the temperatures are the lowest. Both fog and dew disappear (evaporate) as the air temperature rises shortly after sunrise. You also may have noticed that electronic devices such as camcorders come with warnings against bringing them into moist indoors when the devices are cold to avoid moisture condensation on the sensitive electronics of the devices.
It is a common observation that whenever there is an imbalance of a commodity in a medium, nature tends to redistribute it until a "balance" or "equality" is established. This tendency is often referred to as the driving force, which is the mechanism behind many naturally occurring transport phenomena such as heat transfer, fluid flow, electric current, and mass transfer. If we define the amount of a commodity per unit volume as the concentration of that commodity, we can say that the flow of a commodity is always in the direction of decreasing concentration, that is, from the region of high concentration to the region of low concentration (Fig. 3-62). The commodity simply creeps away during redistribution, and thus the flow is a diffusion process.
We know from experience that a wet T-shirt hanging in an open area eventually dries, a small amount of water left in a glass evaporates, and the aftershave in an open bottle quickly disappears. These and many other similar examples suggest that there is a driving force between the two phases of a substance that forces the mass to transform from one phase to another. The magnitude of this force depends on the relative concentrations of the two phases. A wet T-shirt dries much faster in dry air than it would in humid air. In fact, it does not dry at all if the relative humidity of the environment is 100 percent and thus the air is saturated. In this case, there is no transformation from the liquid phase to the vapor phase, and the two phases are in phase equilibrium. For liquid water that is open to the atmosphere, the criterion for phase equilibrium can be expressed as follows: The vapor pressure in the air must be equal to the saturation pressure of water at the water temperature. That is (Fig. 3-63),
Phase equilibrium criterion for water exposed to air: $\quad P_{v}=P_{\text {sat @ } T}$
Therefore, if the vapor pressure in the air is less than the saturation pressure of water at the water temperature, some liquid will evaporate. The larger the difference between the vapor and saturation pressures, the higher the rate of evaporation. The evaporation has a cooling effect on water, and thus reduces its temperature. This, in turn, reduces the saturation pressure of water and thus the rate of evaporation until some kind of quasi-steady operation is reached. This explains why water is usually at a considerably lower temperature than the surrounding air, especially in dry climates. It also suggests that the rate of evaporation of water can be increased by increasing the water temperature and thus the saturation pressure of water.
Note that the air at the water surface is always saturated because of the direct contact with water, and thus the vapor pressure. Therefore, the vapor pressure at the lake surface is the saturation pressure of water at the temperature of the water at the surface. If the air is not saturated, then the vapor pressure decreases to the value in the air at some distance from the water surface, and the difference between these two vapor pressures is the driving force for the evaporation of water.

The natural tendency of water to evaporate in order to achieve phase equilibrium with the water vapor in the surrounding air forms the basis for the
operation of the evaporative coolers (also called the swamp coolers). In such coolers, hot and dry outdoor air is forced to flow through a wet cloth before entering a building. Some of the water evaporates by absorbing heat from the air, and thus cooling it. Evaporative coolers are commonly used in dry climates and provide effective cooling. They are much cheaper to run than air conditioners since they are inexpensive to buy, and the fan of an evaporative cooler consumes much less power than the compressor of an air conditioner.

Boiling and evaporation are often used interchangeably to indicate phase change from liquid to vapor. Although they refer to the same physical process, they differ in some aspects. Evaporation occurs at the liquid-vapor interface when the vapor pressure is less than the saturation pressure of the liquid at a given temperature. Water in a lake at $20^{\circ} \mathrm{C}$, for example, evaporates to air at $20^{\circ} \mathrm{C}$ and 60 percent relative humidity since the saturation pressure of water at $20^{\circ} \mathrm{C}$ is 2.34 kPa , and the vapor pressure of air at $20^{\circ} \mathrm{C}$ and 60 percent relative humidity is 1.4 kPa . Other examples of evaporation are the drying of clothes, fruits, and vegetables; the evaporation of sweat to cool the human body; and the rejection of waste heat in wet cooling towers. Note that evaporation involves no bubble formation or bubble motion (Fig. 3-64).

Boiling, on the other hand, occurs at the solid-liquid interface when a liquid is brought into contact with a surface maintained at a temperature $T_{s}$ sufficiently above the saturation temperature $T_{\text {sat }}$ of the liquid. At 1 atm , for example, liquid water in contact with a solid surface at $110^{\circ} \mathrm{C}$ boils since the saturation temperature of water at 1 atm is $100^{\circ} \mathrm{C}$. The boiling process is characterized by the rapid motion of vapor bubbles that form at the solidliquid interface, detach from the surface when they reach a certain size, and attempt to rise to the free surface of the liquid. When cooking, we do not say water is boiling unless we see the bubbles rising to the top.


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FIGURE 3-64
A liquid-to-vapor phase change process is called evaporation if it occurs at a liquid-vapor interface, and boiling if it occurs at a solid-liquid interface.


FIGURE 3-65
Schematic for Example 3-14.

## EXAMPLE 3-14 Temperature Drop of a Lake Due to Evaporation

On a summer day, the air temperature over a lake is measured to be $25^{\circ} \mathrm{C}$. Determine water temperature of the lake when phase equilibrium conditions are established between the water in the lake and the vapor in the air for relative humidities of 10, 80, and 100 percent for the air (Fig. 3-65).

Solution Air at a specified temperature is blowing over a lake. The equilibrium temperatures of water for three different cases are to be determined.
Analysis The saturation pressure of water at $25^{\circ} \mathrm{C}$, from Table 3-1, is 3.17 kPa . Then the vapor pressures at relative humidities of 10,80 , and 100 percent are determined from Eq. 3-29 to be

$$
\text { Relative humidity }=10 \%: \quad \begin{aligned}
P_{v 1} & =\phi_{1} P_{\text {sat } @ 25^{\circ} \mathrm{C}}=0.1 \times(3.17 \mathrm{kPa}) \\
& =0.317 \mathrm{kPa} \\
\text { Relative humidity }=80 \%: \quad P_{v 2} & =\phi_{2} P_{\text {sat } @ 25^{\circ} \mathrm{C}}=0.8 \times(3.17 \mathrm{kPa}) \\
& =2.536 \mathrm{kPa} \\
& \\
\text { Relative humidity }=100 \%: \quad P_{v 3} & =\phi_{3} P_{\mathrm{sat}} @ 25^{\circ} \mathrm{C}=1.0 \times(3.17 \mathrm{kPa}) \\
& =3.17 \mathrm{kPa}
\end{aligned}
$$

The saturation temperatures corresponding to these pressures are determined from Table 3-1 (or Table A-5) by interpolation to be

$$
T_{1}=-8.0^{\circ} \mathrm{C} \quad T_{2}=21.2^{\circ} \mathrm{C} \quad \text { and } \quad T_{3}=25^{\circ} \mathrm{C}
$$

Therefore, water will freeze in the first case even though the surrounding air is hot. In the last case the water temperature will be the same as the surrounding air temperature.
Discussion You are probably skeptical about the lake freezing when the air is at $25^{\circ} \mathrm{C}$, and you are right. The water temperature drops to $-8^{\circ} \mathrm{C}$ in the limiting case of no heat transfer to the water surface. In practice the water temperature drops below the air temperature, but it does not drop to $-8^{\circ} \mathrm{C}$ because (1) it is very unlikely for the air over the lake to be so dry (a relative humidity of just 10 percent) and (2) as the water temperature near the surface drops, heat transfer from the air and the lower parts of the water body will tend to make up for this heat loss and prevent the water temperature from dropping too much. The water temperature stabilizes when the heat gain from the surrounding air and the water body equals the heat loss by evaporation, that is, when a dynamic balance is established between heat and mass transfer instead of phase equilibrium. If you try this experiment using a shallow layer of water in a well-insulated pan, you can actually freeze the water if the air is very dry and relatively cool.

## SUMMARY

A substance that has a fixed chemical composition throughout is called a pure substance. A pure substance exists in different phases depending on its energy level. In the liquid phase, a substance that is not about to vaporize is called a compressed or subcooled liquid. In the gas phase, a substance that is not about to condense is called a superheated vapor. During a phase-change process, the temperature and pressure of a pure substance are dependent properties. At a given pressure, a substance changes phase at a fixed temperature, called the saturation temperature. Likewise, at a given temperature, the pressure at which a substance changes phase is called the saturation pressure. During a boiling process, both the liquid and the vapor phases coexist in equilibrium, and under this condition the liquid is called saturated liquid and the vapor saturated vapor.

In a saturated liquid-vapor mixture, the mass fraction of vapor is called the quality and is expressed as

$$
x=\frac{m_{\mathrm{vapor}}}{m_{\mathrm{total}}}
$$

Quality may have values between 0 (saturated liquid) and 1 (saturated vapor). It has no meaning in the compressed liquid or superheated vapor regions. In the saturated mixture region, the average value of any intensive property $y$ is determined from

$$
y=y_{f}+x y_{f g}
$$

where $f$ stands for saturated liquid and $g$ for saturated vapor.
In the absence of compressed liquid data, a general approximation is to treat a compressed liquid as a saturated liquid at the given temperature,

$$
y \cong y_{f @ T}
$$

where $y$ stands for $v, u$, or $h$.
The state beyond which there is no distinct vaporization process is called the critical point. At supercritical pressures, a substance gradually and uniformly expands from the liquid to vapor phase. All three phases of a substance coexist in equilibrium at states along the triple line characterized by triple-line temperature and pressure. The compressed liquid has lower $v, u$, and $h$ values than the saturated liquid at the same $T$ or $P$. Likewise, superheated vapor has higher $v, u$, and $h$ values than the saturated vapor at the same $T$ or $P$.

Any relation among the pressure, temperature, and specific volume of a substance is called an equation of state. The simplest and best-known equation of state is the ideal-gas equation of state, given as

$$
P v=R T
$$

where $R$ is the gas constant. Caution should be exercised in using this relation since an ideal gas is a fictitious substance.

Real gases exhibit ideal-gas behavior at relatively low pressures and high temperatures.
The deviation from ideal-gas behavior can be properly accounted for by using the compressibility factor $Z$, defined as

$$
Z=\frac{P V}{R T} \quad \text { or } \quad Z=\frac{V_{\text {actual }}}{V_{\text {ideal }}}
$$

The $Z$ factor is approximately the same for all gases at the same reduced temperature and reduced pressure, which are defined as

$$
T_{R}=\frac{T}{T_{\mathrm{cr}}} \quad \text { and } \quad P_{R}=\frac{P}{P_{\mathrm{cr}}}
$$

where $P_{\text {cr }}$ and $T_{\text {cr }}$ are the critical pressure and temperature, respectively. This is known as the principle of corresponding states. When either $P$ or $T$ is unknown, it can be determined from the compressibility chart with the help of the pseudoreduced specific volume, defined as

$$
V_{R}=\frac{V_{\text {actual }}}{R T_{\mathrm{cr}} / P_{\mathrm{cr}}}
$$

The $P-V-T$ behavior of substances can be represented more accurately by more complex equations of state. Three of the best known are
van der Waals: $\quad\left(P+\frac{a}{v^{2}}\right)(v-b)=R T$
where

$$
a=\frac{27 R^{2} T_{\mathrm{cr}}^{2}}{64 P_{\mathrm{cr}}} \quad \text { and } \quad b=\frac{R T_{\text {cr }}}{8 P_{\mathrm{cr}}}
$$

Beattie-Bridgeman: $\quad P=\frac{R_{u} T}{\bar{V}^{2}}\left(1-\frac{c}{\bar{V} T^{3}}\right)(\bar{v}+B)-\frac{A}{\bar{V}^{2}}$
where

$$
A=A_{0}\left(1-\frac{a}{\bar{V}}\right) \quad \text { and } \quad B=B_{0}\left(1-\frac{b}{\bar{V}}\right)
$$

Benedict-Webb-Rubin:

$$
\begin{aligned}
P= & \frac{R_{u} T}{\bar{V}}+\left(B_{0} R_{u} T-A_{0}-\frac{C_{0}}{T^{2}}\right) \frac{1}{\bar{V}^{2}}+\frac{b R_{u} T-a}{\bar{v}^{3}}+\frac{a \alpha}{\bar{V}^{6}} \\
& +\frac{c}{\bar{V}^{3} T^{2}}\left(1+\frac{\gamma}{\bar{V}^{2}}\right) e^{-\gamma / \bar{V}^{2}}
\end{aligned}
$$

where $R_{u}$ is the universal gas constant and $\bar{v}$ is the molar specific volume.

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## REFERENGES AND SUGGESTED READINGS

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3. A. Bejan. Advanced Engineering Thermodynamics. 2nd ed. New York: Wiley, 1997.
4. M. Kostic. Analysis of Enthalpy Approximation for Compressed Liquid Water. IMECE 2004, ASME Proceedings, ASME, New York, 2004.

## PROBLEMS*

## Pure Substances, Phase-Change Processes, Property Diagrams

3-1C Is iced water a pure substance? Why?
3-2C What is the difference between saturated liquid and compressed liquid?

3-3C What is the difference between saturated vapor and superheated vapor?
3-4C Is there any difference between the intensive properties of saturated vapor at a given temperature and the vapor of a saturated mixture at the same temperature?
3-5C Is there any difference between the intensive properties of saturated liquid at a given temperature and the liquid of a saturated mixture at the same temperature?

3-6C Is it true that water boils at higher temperatures at higher pressures? Explain.
3-7C If the pressure of a substance is increased during a boiling process, will the temperature also increase or will it remain constant? Why?
3-8C Why are the temperature and pressure dependent properties in the saturated mixture region?
3-9C What is the difference between the critical point and the triple point?
3-10C Is it possible to have water vapor at $-10^{\circ} \mathrm{C}$ ?
3-11C A househusband is cooking beef stew for his family in a pan that is (a) uncovered, (b) covered with a light lid, and (c) covered with a heavy lid. For which case will the cooking time be the shortest? Why?

[^3]3-12C How does the boiling process at supercritical pressures differ from the boiling process at subcritical pressures?

## Property Tables

3-13C In what kind of pot will a given volume of water boil at a higher temperature: a tall and narrow one or a short and wide one? Explain.

3-14C A perfectly fitting pot and its lid often stick after cooking, and it becomes very difficult to open the lid when the pot cools down. Explain why this happens and what you would do to open the lid.
3-15C It is well known that warm air in a cooler environment rises. Now consider a warm mixture of air and gasoline on top of an open gasoline can. Do you think this gas mixture will rise in a cooler environment?
3-16C In 1775, Dr. William Cullen made ice in Scotland by evacuating the air in a water tank. Explain how that device works, and discuss how the process can be made more efficient.
3-17C Does the amount of heat absorbed as 1 kg of saturated liquid water boils at $100^{\circ} \mathrm{C}$ have to be equal to the amount of heat released as 1 kg of saturated water vapor condenses at $100^{\circ} \mathrm{C}$ ?

3-18C Does the reference point selected for the properties of a substance have any effect on thermodynamic analysis? Why?
3-19C What is the physical significance of $h_{f g}$ ? Can it be obtained from a knowledge of $h_{f}$ and $h_{g}$ ? How?
3-20C Is it true that it takes more energy to vaporize 1 kg of saturated liquid water at $100^{\circ} \mathrm{C}$ than it would at $120^{\circ} \mathrm{C}$ ?
3-21C What is quality? Does it have any meaning in the superheated vapor region?
3-22C Which process requires more energy: completely vaporizing 1 kg of saturated liquid water at 1 atm pressure or completely vaporizing 1 kg of saturated liquid water at 8 atm pressure?
3-23C Does $h_{f g}$ change with pressure? How?

3-24C Can quality be expressed as the ratio of the volume occupied by the vapor phase to the total volume? Explain.
$\mathbf{3 - 2 5 C}$ In the absence of compressed liquid tables, how is the specific volume of a compressed liquid at a given $P$ and $T$ determined?

| T, ${ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $\mathrm{v}, \mathrm{m}^{3} / \mathrm{kg}$ | Phase description |
| :---: | :---: | :---: | :---: |
| 50 |  | 4.16 |  |
|  | 200 | Saturated vapor |  |
| 250 | 400 |  |  |
| 110 | 600 |  |  |

3-27 世GS Reconsider Prob. 3-26. Using EES (or other) software, determine the missing properties of water. Repeat the solution for refrigerant-134a, refrigerant22, and ammonia.
3-28E Complete this table for $\mathrm{H}_{2} \mathrm{O}$ :

| $T,{ }^{\circ} \mathrm{F}$ | $P$, psia | $u$, Btu/lbm | Phase description |
| :--- | :--- | :--- | :--- |
| 300 |  | 782 |  |
|  | 40 |  | Saturated liquid |
| 500 | 120 |  |  |
| 400 | 400 |  |  |

3-29E EGS Reconsider Prob. 3-28E. Using EES (or other) software, determine the missing properties of water. Repeat the solution for refrigerant-134a, refrigerant22, and ammonia.

| $\underline{T, ~}{ }^{\circ} \mathrm{C}$ | P, kPa | $h, \mathrm{~kJ} / \mathrm{kg}$ | $x$ | Phase description |
| :---: | :---: | :---: | :---: | :---: |
|  | 200 | 0.7 |  |  |
| 140 |  | 1800 |  |  |
|  | 950 | 0.0 |  |  |
| 80 | 500 |  |  |  |
|  | 800 | 3162.2 |  |  |

3-31 Complete this table for refrigerant-134a:

| $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $\mathrm{v}, \mathrm{m}^{3} / \mathrm{kg}$ | Phase description |
| :---: | :---: | :---: | :---: |
| -8 | 320 |  |  |
| 30 |  | 0.015 |  |
| 80 | 180 |  |  |
| $\mathbf{3 - 3 2}$ | Complete this table for refrigerant-134a: |  |  |
| $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $u, \mathrm{~kJ} / \mathrm{kg}$ | Phase description |
| 20 |  | 95 |  |
| -12 |  |  | Saturated liquid |
|  | 400 | 300 |  |
| 8 | 600 |  |  |

3-33E Complete this table for refrigerant-134a:

| $T,{ }^{\circ} \mathrm{F}$ | $P$, psia | $h$, Btu/lbm | $x$ | Phase description |
| :---: | :---: | :---: | :---: | :---: |
|  | 80 | 78 |  |  |
| 15 |  |  | 0.6 |  |
| 10 | 70 |  |  |  |
|  | 180 | 129.46 |  |  |
| 110 |  |  | 1.0 |  |

3-34 Complete this table for $\mathrm{H}_{2} \mathrm{O}$ :

| $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $\mathrm{v}, \mathrm{m}^{3} / \mathrm{kg}$ | Phase description |
| :---: | :---: | :---: | :---: |
| 140 |  | 0.05 |  |
|  | 550 |  | Saturated liquid |
| 125 | 750 |  |  |
| 500 |  | 0.140 |  |

3-35 Complete this table for $\mathrm{H}_{2} \mathrm{O}$ :

| $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $u, \mathrm{~kJ} / \mathrm{kg}$ | Phase description |
| :--- | :---: | :---: | :---: |
|  | 400 | 1450 |  |
| 220 |  |  | Saturated vapor |
| 190 | 2500 |  |  |
|  | 4000 | 3040 |  |

3-36 A $1.8-\mathrm{m}^{3}$ rigid tank contains steam at $220^{\circ} \mathrm{C}$. Onethird of the volume is in the liquid phase and the rest is in the vapor form. Determine (a) the pressure of the steam, (b) the quality of the saturated mixture, and (c) the density of the mixture.


FIGURE P3-36

3-37 A piston-cylinder device contains 0.85 kg of refrigerant134 a at $-10^{\circ} \mathrm{C}$. The piston that is free to move has a mass of 12 kg and a diameter of 25 cm . The local atmospheric pressure is 88 kPa . Now, heat is transferred to refrigerant-134a


FIGURE P3-37

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until the temperature is $15^{\circ} \mathrm{C}$. Determine (a) the final pressure, (b) the change in the volume of the cylinder, and (c) the change in the enthalpy of the refrigerant-134a.
3-38E The temperature in a pressure cooker during cooking at sea level is measured to be $250^{\circ} \mathrm{F}$. Determine the absolute pressure inside the cooker in psia and in atm. Would you modify your answer if the place were at a higher elevation?


FIGURE P3-38E

3-39E The atmospheric pressure at a location is usually specified at standard conditions, but it changes with the weather conditions. As the weather forecasters frequently state, the atmospheric pressure drops during stormy weather and it rises during clear and sunny days. If the pressure difference between the two extreme conditions is given to be 0.3 in of mercury, determine how much the boiling temperatures of water will vary as the weather changes from one extreme to the other.
3-40 A person cooks a meal in a $30-\mathrm{cm}$-diameter pot that is covered with a well-fitting lid and lets the food cool to the room temperature of $20^{\circ} \mathrm{C}$. The total mass of the food and the pot is 8 kg . Now the person tries to open the pan by lifting the lid up. Assuming no air has leaked into the pan during cooling, determine if the lid will open or the pan will move up together with the lid.
3-41 Water is to be boiled at sea level in a $30-\mathrm{cm}$-diameter stainless steel pan placed on top of a $3-\mathrm{kW}$ electric burner. If


FIGURE P3-41

60 percent of the heat generated by the burner is transferred to the water during boiling, determine the rate of evaporation of water.
3-42 Repeat Prob. 3-41 for a location at an elevation of 1500 m where the atmospheric pressure is 84.5 kPa and thus the boiling temperature of water is $95^{\circ} \mathrm{C}$.
3-43 Water is boiled at 1 atm pressure in a $25-\mathrm{cm}$-internaldiameter stainless steel pan on an electric range. If it is observed that the water level in the pan drops by 10 cm in 45 min , determine the rate of heat transfer to the pan.

3-44 Repeat Prob. 3-43 for a location at 2000-m elevation where the standard atmospheric pressure is 79.5 kPa .
3-45 Saturated steam coming off the turbine of a steam power plant at $30^{\circ} \mathrm{C}$ condenses on the outside of a $3-\mathrm{cm}$ -outer-diameter, $35-\mathrm{m}$-long tube at a rate of $45 \mathrm{~kg} / \mathrm{h}$. Determine the rate of heat transfer from the steam to the cooling water flowing through the pipe.
3-46 The average atmospheric pressure in Denver (elevation $=1610 \mathrm{~m}$ ) is 83.4 kPa . Determine the temperature at which water in an uncovered pan boils in Denver.
Answer: $94.6^{\circ} \mathrm{C}$.
3-47 Water in a $5-\mathrm{cm}$-deep pan is observed to boil at $98^{\circ} \mathrm{C}$. At what temperature will the water in a $40-\mathrm{cm}$-deep pan boil? Assume both pans are full of water.
3-48 A cooking pan whose inner diameter is 20 cm is filled with water and covered with a $4-\mathrm{kg}$ lid. If the local atmospheric pressure is 101 kPa , determine the temperature at which the water starts boiling when it is heated.
Answer: $100.2^{\circ} \mathrm{C}$


FIGURE P3-48

3-49 EGS Reconsider Prob. 3-48. Using EES (or other) software, investigate the effect of the mass of the lid on the boiling temperature of water in the pan. Let the mass vary from 1 kg to 10 kg . Plot the boiling temperature against the mass of the lid, and discuss the results.
3-50 Water is being heated in a vertical piston-cylinder device. The piston has a mass of 20 kg and a cross-sectional area of $100 \mathrm{~cm}^{2}$. If the local atmospheric pressure is 100 kPa , determine the temperature at which the water starts boiling.

3-51 A rigid tank with a volume of $2.5 \mathrm{~m}^{3}$ contains 15 kg of saturated liquid-vapor mixture of water at $75^{\circ} \mathrm{C}$. Now the water is slowly heated. Determine the temperature at which the liquid in the tank is completely vaporized. Also, show the process on a $T-V$ diagram with respect to saturation lines. Answer: $187.0^{\circ} \mathrm{C}$
3-52 A rigid vessel contains 2 kg of refrigerant-134a at 800 kPa and $120^{\circ} \mathrm{C}$. Determine the volume of the vessel and the total internal energy. Answers: $0.0753 \mathrm{~m}^{3}, 655.7 \mathrm{~kJ}$
3-53E A 5-ft ${ }^{3}$ rigid tank contains 5 lbm of water at 20 psia . Determine $(a)$ the temperature, $(b)$ the total enthalpy, and $(c)$ the mass of each phase of water.
3-54 A $0.5-\mathrm{m}^{3}$ vessel contains 10 kg of refrigerant-134a at $-20^{\circ} \mathrm{C}$. Determine (a) the pressure, (b) the total internal energy, and (c) the volume occupied by the liquid phase. Answers: (a) $132.82 \mathrm{kPa},(b) 904.2 \mathrm{~kJ}$, (c) $0.00489 \mathrm{~m}^{3}$

3-55 A piston-cylinder device contains $0.1 \mathrm{~m}^{3}$ of liq(©) uid water and $0.9 \mathrm{~m}^{3}$ of water vapor in equilibrium at 800 kPa . Heat is transferred at constant pressure until the temperature reaches $350^{\circ} \mathrm{C}$.
(a) What is the initial temperature of the water?
(b) Determine the total mass of the water.
(c) Calculate the final volume.
(d) Show the process on a $P-\vee$ diagram with respect to saturation lines.


FIGURE P3-55

3-56 € $\Subset$ Reconsider Prob. 3-55. Using EES (or other) software, investigate the effect of pressure on the total mass of water in the tank. Let the pressure vary from 0.1 MPa to 1 MPa . Plot the total mass of water against pressure, and discuss the results. Also, show the process in Prob. 3-55 on a $P-\vee$ diagram using the property plot feature of EES.
3-57E Superheated water vapor at 180 psia and $500^{\circ} \mathrm{F}$ is allowed to cool at constant volume until the temperature drops to $250^{\circ} \mathrm{F}$. At the final state, determine (a) the pressure, (b) the quality, and (c) the enthalpy. Also, show the process on a $T-v$ diagram with respect to saturation lines. Answers: (a) 29.84 psia, (b) 0.219 , (c) 426.0 Btu/lbm Reconsider Prob. 3-57E. Using EES (or other) software, investigate the effect of initial pressure on the quality of water at the final state. Let the pressure vary from 100 psi to 300 psi. Plot the quality against initial pressure, and discuss the results. Also, show the process in Prob. 3-57E on a $T-v$ diagram using the property plot feature of EES.

3-59 A piston-cylinder device initially contains 50 L of liquid water at $40^{\circ} \mathrm{C}$ and 200 kPa . Heat is transferred to the water at constant pressure until the entire liquid is vaporized.
(a) What is the mass of the water?
(b) What is the final temperature?
(c) Determine the total enthalpy change.
(d) Show the process on a $T-v$ diagram with respect to saturation lines.
Answers: (a) 49.61 kg , (b) $120.21^{\circ} \mathrm{C}$, (c) $125,943 \mathrm{~kJ}$
3-60 A $0.3-\mathrm{m}^{3}$ rigid vessel initially contains saturated liquidvapor mixture of water at $150^{\circ} \mathrm{C}$. The water is now heated until it reaches the critical state. Determine the mass of the liquid water and the volume occupied by the liquid at the initial state. Answers: $96.10 \mathrm{~kg}, 0.105 \mathrm{~m}^{3}$
3-61 Determine the specific volume, internal energy, and enthalpy of compressed liquid water at $100^{\circ} \mathrm{C}$ and 15 MPa using the saturated liquid approximation. Compare these values to the ones obtained from the compressed liquid tables.

Reconsider Prob. 3-61. Using EES (or other) software, determine the indicated properties of compressed liquid, and compare them to those obtained using the saturated liquid approximation.
3-63E A $15-\mathrm{ft}^{3}$ rigid tank contains a saturated mixture of refrigerant-134a at 50 psia . If the saturated liquid occupies 20 percent of the volume, determine the quality and the total mass of the refrigerant in the tank.
3-64 A piston-cylinder device contains 0.8 kg of steam at $300^{\circ} \mathrm{C}$ and 1 MPa . Steam is cooled at constant pressure until one-half of the mass condenses.
(a) Show the process on a $T-\vee$ diagram.
(b) Find the final temperature.
(c) Determine the volume change.

3-65 A rigid tank contains water vapor at $250^{\circ} \mathrm{C}$ and an unknown pressure. When the tank is cooled to $150^{\circ} \mathrm{C}$, the vapor starts condensing. Estimate the initial pressure in the tank. Answer: 0.60 MPa
3-66 Water is boiled in a pan covered with a poorly fitting lid at a specified location. Heat is supplied to the pan by a $2-\mathrm{kW}$ resistance heater. The amount of water in the pan is observed to decrease by 1.19 kg in 30 minutes. If it is estimated that 75 percent of electricity consumed by the heater is transferred to the water as heat, determine the local atmospheric pressure in that location. Answer: 85.4 kPa

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3-67 A rigid tank initially contains $1.4-\mathrm{kg}$ saturated liquid water at $200^{\circ} \mathrm{C}$. At this state, 25 percent of the volume is occupied by water and the rest by air. Now heat is supplied to the water until the tank contains saturated vapor only. Determine (a) the volume of the tank, (b) the final temperature and pressure, and $(c)$ the internal energy change of the water.


FIGURE P3-67

3-68 A piston-cylinder device initially contains steam at 3.5 MPa , superheated by $5^{\circ} \mathrm{C}$. Now, steam loses heat to the surroundings and the piston moves down hitting a set of stops at which point the cylinder contains saturated liquid water. The cooling continues until the cylinder contains water at $200^{\circ} \mathrm{C}$. Determine (a) the initial temperature, (b) the enthalpy change per unit mass of the steam by the time the piston first hits the stops, and (c) the final pressure and the quality (if mixture).


FIGURE P3-68

## Ideal Gas

3-69C Propane and methane are commonly used for heating in winter, and the leakage of these fuels, even for short periods, poses a fire danger for homes. Which gas leakage do you think poses a greater risk for fire? Explain.
3-70C Under what conditions is the ideal-gas assumption suitable for real gases?
3-71C What is the difference between $R$ and $R_{u}$ ? How are these two related?

3-72C What is the difference between mass and molar mass? How are these two related?
3-73 A spherical balloon with a diameter of 6 m is filled with helium at $20^{\circ} \mathrm{C}$ and 200 kPa . Determine the mole number and the mass of the helium in the balloon. Answers: 9.28 kmol, 37.15 kg Reconsider Prob. 3-73. Using EES (or other) software, investigate the effect of the balloon diameter on the mass of helium contained in the balloon for the pressures of (a) 100 kPa and (b) 200 kPa . Let the diameter vary from 5 m to 15 m . Plot the mass of helium against the diameter for both cases.

3-75 The pressure in an automobile tire depends on the temperature of the air in the tire. When the air temperature is $25^{\circ} \mathrm{C}$, the pressure gage reads 210 kPa . If the volume of the tire is $0.025 \mathrm{~m}^{3}$, determine the pressure rise in the tire when the air temperature in the tire rises to $50^{\circ} \mathrm{C}$. Also, determine the amount of air that must be bled off to restore pressure to its original value at this temperature. Assume the atmospheric pressure is 100 kPa .


FIGURE P3-75

3-76E The air in an automobile tire with a volume of 0.53 $\mathrm{ft}^{3}$ is at $90^{\circ} \mathrm{F}$ and 20 psig . Determine the amount of air that must be added to raise the pressure to the recommended value of 30 psig . Assume the atmospheric pressure to be 14.6 psia and the temperature and the volume to remain constant. Answer: 0.0260 lbm
3-77 The pressure gage on a $2.5-\mathrm{m}^{3}$ oxygen tank reads 500 kPa . Determine the amount of oxygen in the tank if the temperature is $28^{\circ} \mathrm{C}$ and the atmospheric pressure is 97 kPa .


FIGURE P3-77

3-78E A rigid tank contains 20 lbm of air at 20 psia and $70^{\circ} \mathrm{F}$. More air is added to the tank until the pressure and temperature rise to 35 psia and $90^{\circ} \mathrm{F}$, respectively. Determine the amount of air added to the tank. Answer: 13.73 lbm
3-79 A 400-L rigid tank contains 5 kg of air at $25^{\circ} \mathrm{C}$. Determine the reading on the pressure gage if the atmospheric pressure is 97 kPa .
3-80 A $1-\mathrm{m}^{3}$ tank containing air at $25^{\circ} \mathrm{C}$ and 500 kPa is connected through a valve to another tank containing 5 kg of air at $35^{\circ} \mathrm{C}$ and 200 kPa . Now the valve is opened, and the entire system is allowed to reach thermal equilibrium with the surroundings, which are at $20^{\circ} \mathrm{C}$. Determine the volume of the second tank and the final equilibrium pressure of air. Answers: $2.21 \mathrm{~m}^{3}, 284.1 \mathrm{kPa}$

## Compressibility Factor

3-81C What is the physical significance of the compressibility factor $Z$ ?
3-82C What is the principle of corresponding states?
3-83C How are the reduced pressure and reduced temperature defined?
3-84 Determine the specific volume of superheated water vapor at 10 MPa and $400^{\circ} \mathrm{C}$, using (a) the ideal-gas equation, (b) the generalized compressibility chart, and (c) the steam tables. Also determine the error involved in the first two cases. Answers: (a) $0.03106 \mathrm{~m}^{3} / \mathrm{kg}, 17.6$ percent; (b) $0.02609 \mathrm{~m}^{3} / \mathrm{kg}$, 1.2 percent; (c) $0.02644 \mathrm{~m}^{3} / \mathrm{kg}$

3-85 EGS Reconsider Prob. 3-84. Solve the problem using the generalized compressibility factor feature of the EES software. Again using EES, compare the specific volume of water for the three cases at 10 MPa over the temperature range of 325 to $600^{\circ} \mathrm{C}$ in $25^{\circ} \mathrm{C}$ intervals. Plot the percent error involved in the ideal-gas approximation against temperature, and discuss the results.
3-86 Determine the specific volume of refrigerant-134a vapor at 0.9 MPa and $70^{\circ} \mathrm{C}$ based on (a) the ideal-gas equation, (b) the generalized compressibility chart, and (c) data from tables. Also, determine the error involved in the first two cases.

3-87 Determine the specific volume of nitrogen gas at 10 MPa and 150 K based on (a) the ideal-gas equation and (b) the generalized compressibility chart. Compare these results with the experimental value of $0.002388 \mathrm{~m}^{3} / \mathrm{kg}$, and determine the error involved in each case. Answers: (a) $0.004452 \mathrm{~m}^{3} / \mathrm{kg}$, 86.4 percent; (b) $0.002404 \mathrm{~m}^{3} / \mathrm{kg}, 0.7$ percent

3-88 Determine the specific volume of superheated water vapor at 3.5 MPa and $450^{\circ} \mathrm{C}$ based on (a) the ideal-gas equation, (b) the generalized compressibility chart, and (c) the steam tables. Determine the error involved in the first two cases.

3-89E Refrigerant-134a at 400 psia has a specific volume of $0.13853 \mathrm{ft}^{3} / \mathrm{lbm}$. Determine the temperature of the refrigerant based on (a) the ideal-gas equation, (b) the generalized compressibility chart, and (c) the refrigerant tables.
3-90 A $0.016773-\mathrm{m}^{3}$ tank contains 1 kg of refrigerant-134a at $110^{\circ} \mathrm{C}$. Determine the pressure of the refrigerant, using (a) the ideal-gas equation, (b) the generalized compressibility chart, and (c) the refrigerant tables. Answers: (a) 1.861 MPa , (b) 1.583 MPa , (c) 1.6 MPa

3-91 Somebody claims that oxygen gas at 160 K and 3 MPa can be treated as an ideal gas with an error of less than 10 percent. Is this claim valid?
3-92 What is the percentage of error involved in treating carbon dioxide at 3 MPa and $10^{\circ} \mathrm{C}$ as an ideal gas? Answer: 25 percent
3-93 What is the percentage of error involved in treating carbon dioxide at 7 MPa and 380 K as an ideal gas?
3-94 Carbon dioxide gas enters a pipe at 3 MPa and 500 K at a rate of $2 \mathrm{~kg} / \mathrm{s} . \mathrm{CO}_{2}$ is cooled at constant pressure as it flows in the pipe and the temperature $\mathrm{CO}_{2}$ drops to 450 K at the exit. Determine the volume flow rate and the density of carbon dioxide at the inlet and the volume flow rate at the exit of the pipe using (a) the ideal-gas equation and (b) the generalized compressibility chart. Also, determine (c) the error involved in each case.


## Other Equations of State

3-95C What is the physical significance of the two constants that appear in the van der Waals equation of state? On what basis are they determined?
3-96 A $3.27-\mathrm{m}^{3}$ tank contains 100 kg of nitrogen at 175 K . Determine the pressure in the tank, using (a) the ideal-gas equation, (b) the van der Waals equation, and (c) the BeattieBridgeman equation. Compare your results with the actual value of 1505 kPa .
3-97 A $1-\mathrm{m}^{3}$ tank contains 2.841 kg of steam at 0.6 MPa . Determine the temperature of the steam, using (a) the idealgas equation, (b) the van der Waals equation, and (c) the steam tables. Answers: (a) 457.6 K , (b) 465.9 K , (c) 473 K
3-98 EGS Reconsider Prob. 3-97. Solve the problem using EES (or other) software. Again using the EES, compare the temperature of water for the three cases at constant specific volume over the pressure range of 0.1 MPa to

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1 MPa in 0.1 MPa increments. Plot the percent error involved in the ideal-gas approximation against pressure, and discuss the results.
3-99E Refrigerant-134a at 100 psia has a specific volume of $0.54022 \mathrm{ft}^{3} / \mathrm{lbm}$. Determine the temperature of the refrigerant based on (a) the ideal-gas equation, (b) the van der Waals equation, and (c) the refrigerant tables.
3-100 Nitrogen at 150 K has a specific volume of $0.041884 \mathrm{~m}^{3} / \mathrm{kg}$. Determine the pressure of the nitrogen, using (a) the ideal-gas equation and $(b)$ the BeattieBridgeman equation. Compare your results to the experimental value of 1000 kPa . Answers: (a) 1063 kPa , (b) 1000.4 kPa
3-101 e¢S Reconsider Prob. 3-100. Using EES (or other) software, compare the pressure results of the ideal-gas and Beattie-Bridgeman equations with nitrogen data supplied by EES. Plot temperature versus specific volume for a pressure of 1000 kPa with respect to the saturated liquid and saturated vapor lines of nitrogen over the range of $110 \mathrm{~K}<T<150 \mathrm{~K}$.

## Special Topic: Vapor Pressure and Phase Equilibrium

3-102 Consider a glass of water in a room that is at $20^{\circ} \mathrm{C}$ and 60 percent relative humidity. If the water temperature is $15^{\circ} \mathrm{C}$, determine the vapor pressure $(a)$ at the free surface of the water and $(b)$ at a location in the room far from the glass.
3-103 During a hot summer day at the beach when the air temperature is $30^{\circ} \mathrm{C}$, someone claims the vapor pressure in the air to be 5.2 kPa . Is this claim reasonable?
3-104 On a certain day, the temperature and relative humidity of air over a large swimming pool are measured to be $20^{\circ} \mathrm{C}$ and 40 percent, respectively. Determine the water temperature of the pool when phase equilibrium conditions are established between the water in the pool and the vapor in the air.
3-105 Consider two rooms that are identical except that one is maintained at $30^{\circ} \mathrm{C}$ and 40 percent relative humidity while the other is maintained at $20^{\circ} \mathrm{C}$ and 70 percent relative humidity. Noting that the amount of moisture is proportional to the vapor pressure, determine which room contains more moisture.
3-106E A thermos bottle is half-filled with water and is left open to the atmospheric air at $70^{\circ} \mathrm{F}$ and 35 percent relative humidity. If heat transfer to the water through the thermos walls and the free surface is negligible, determine the temperature of water when phase equilibrium is established.
3-107 During a hot summer day when the air temperature is $35^{\circ} \mathrm{C}$ and the relative humidity is 70 percent, you buy a supposedly "cold" canned drink from a store. The store owner claims that the temperature of the drink is below $10^{\circ} \mathrm{C}$. Yet the drink does not feel so cold and you are skeptical
since you notice no condensation forming outside the can. Can the store owner be telling the truth?

## Review Problems

3-108 The combustion in a gasoline engine may be approximated by a constant volume heat addition process. There exists the air-fuel mixture in the cylinder before the combustion and the combustion gases after it, and both may be approximated as air, an ideal gas. In a gasoline engine, the cylinder conditions are 1.8 MPa and $450^{\circ} \mathrm{C}$ before the combustion and $1300^{\circ} \mathrm{C}$ after it. Determine the pressure at the end of the combustion process. Answer: 3916 kPa


FIGURE P3-108
3-109 A rigid tank contains an ideal gas at 300 kPa and 600 K . Now half of the gas is withdrawn from the tank and the gas is found at 100 kPa at the end of the process. Determine (a) the final temperature of the gas and (b) the final pressure if no mass was withdrawn from the tank and the same final temperature was reached at the end of the process.


FIGURE P3-109

3-110 Carbon-dioxide gas at 3 MPa and 500 K flows steadily in a pipe at a rate of $0.4 \mathrm{kmol} / \mathrm{s}$. Determine (a) the volume and mass flow rates and the density of carbon dioxide at this state. If $\mathrm{CO}_{2}$ is cooled at constant pressure as


FIGURE P3-110
it flows in the pipe so that the temperature of $\mathrm{CO}_{2}$ drops to 450 K at the exit of the pipe, determine (b) the volume flow rate at the exit of the pipe.
3-111 A piston-cylinder device initially contains 0.2 kg of steam at 200 kPa and $300^{\circ} \mathrm{C}$. Now, the steam is cooled at constant pressure until it is at $150^{\circ} \mathrm{C}$. Determine the volume change of the cylinder during this process using the compressibility factor and compare the result to the actual value.


FIGURE P3-111

3-112 Combustion in a diesel engine may be modeled as a constant-pressure heat addition process with air in the cylinder before and after combustion. Consider a diesel engine with cylinder conditions of 950 K and $75 \mathrm{~cm}^{3}$ before combustion, and $150 \mathrm{~cm}^{3}$ after it. The engine operates with an air-fuel ratio of 22 kg air $/ \mathrm{kg}$ fuel (the mass of the air divided by the mass of the fuel). Determine the temperature after the combustion process.


FIGURE P3-112
3-113 On the property diagrams indicated below, sketch (not to scale) with respect to the saturated liquid and saturated vapor lines and label the following processes and states for steam. Use arrows to indicate the direction of the process, and label the initial and final states:
(a) On the $P-V$ diagram sketch the constant temperature process through the state $P=300 \mathrm{kPa}, v=0.525 \mathrm{~m}^{3} / \mathrm{kg}$ as pressure changes from $P_{1}=200 \mathrm{kPa}$ to $P_{2}=400 \mathrm{kPa}$. Place the value of the temperature on the process curve on the $P-\vee$ diagram.
(b) On the $T-V$ diagram sketch the constant specific volume process through the state $T=120^{\circ} \mathrm{C}, v=0.7163 \mathrm{~m}^{3} / \mathrm{kg}$ from $P_{1}=100 \mathrm{kPa}$ to $P_{2}=300 \mathrm{kPa}$. For this data set place the temperature values at states 1 and 2 on its axis. Place the value of the specific volume on its axis.
3-114 The gage pressure of an automobile tire is measured to be 200 kPa before a trip and 220 kPa after the trip at a location where the atmospheric pressure is 90 kPa . Assuming the volume of the tire remains constant at $0.035 \mathrm{~m}^{3}$, determine the percent increase in the absolute temperature of the air in the tire.
3-115 Although balloons have been around since 1783 when the first balloon took to the skies in France, a real breakthrough in ballooning occurred in 1960 with the design of the modern hot-air balloon fueled by inexpensive propane and constructed of lightweight nylon fabric. Over the years, ballooning has become a sport and a hobby for many people around the world. Unlike balloons filled with the light helium gas, hot-air balloons are open to the atmosphere. Therefore, the pressure in the balloon is always the same as the local atmospheric pressure, and the balloon is never in danger of exploding.

Hot-air balloons range from about 15 to 25 m in diameter. The air in the balloon cavity is heated by a propane burner located at the top of the passenger cage. The flames from the burner that shoot into the balloon heat the air in the balloon cavity, raising the air temperature at the top of the balloon from $65^{\circ} \mathrm{C}$ to over $120^{\circ} \mathrm{C}$. The air temperature is maintained at the desired levels by periodically firing the propane burner.


FIGURE P3-115
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The buoyancy force that pushes the balloon upward is proportional to the density of the cooler air outside the balloon and the volume of the balloon, and can be expressed as

$$
F_{B}=\rho_{\text {cool air }} g V_{\text {balloon }}
$$

where $g$ is the gravitational acceleration. When air resistance is negligible, the buoyancy force is opposed by (1) the weight of the hot air in the balloon, (2) the weight of the cage, the ropes, and the balloon material, and (3) the weight of the people and other load in the cage. The operator of the balloon can control the height and the vertical motion of the balloon by firing the burner or by letting some hot air in the balloon escape, to be replaced by cooler air. The forward motion of the balloon is provided by the winds.

Consider a $20-\mathrm{m}$-diameter hot-air balloon that, together with its cage, has a mass of 80 kg when empty. This balloon is hanging still in the air at a location where the atmospheric pressure and temperature are 90 kPa and $15^{\circ} \mathrm{C}$, respectively, while carrying three $65-\mathrm{kg}$ people. Determine the average temperature of the air in the balloon. What would your response be if the atmospheric air temperature were $30^{\circ} \mathrm{C}$ ?
3-116 ©GS Reconsider Prob. 3-115. Using EES (or other) software, investigate the effect of the environment temperature on the average air temperature in the balloon when the balloon is suspended in the air. Assume the environment temperature varies from -10 to $30^{\circ} \mathrm{C}$. Plot the average air temperature in the balloon versus the environment temperature, and discuss the results. Investigate how the number of people carried affects the temperature of the air in the balloon.
3-117 Consider an 18-m-diameter hot-air balloon that, together with its cage, has a mass of 120 kg when empty. The air in the balloon, which is now carrying two $70-\mathrm{kg}$ people, is heated by propane burners at a location where the atmospheric pressure and temperature are 93 kPa and $12^{\circ} \mathrm{C}$, respectively. Determine the average temperature of the air in the balloon when the balloon first starts rising. What would your response be if the atmospheric air temperature were $25^{\circ} \mathrm{C}$ ?
3-118E Water in a pressure cooker is observed to boil at $260^{\circ} \mathrm{F}$. What is the absolute pressure in the pressure cooker, in psia?
3-119 A rigid tank with a volume of $0.117 \mathrm{~m}^{3}$ contains 1 kg of refrigerant-134a vapor at 240 kPa . The refrigerant is now allowed to cool. Determine the pressure when the refrigerant first starts condensing. Also, show the process on a $P-\vee$ diagram with respect to saturation lines.
3-120 A 4-L rigid tank contains 2 kg of saturated liquid-vapor mixture of water at $50^{\circ} \mathrm{C}$. The water is now slowly heated until it exists in a single phase. At the final state, will the water be in the liquid phase or the vapor phase? What would your answer be if the volume of the tank were 400 L instead of 4 L ?


FIGURE P3-120
3-121 A $10-\mathrm{kg}$ mass of superheated refrigerant-134a at 1.2 MPa and $70^{\circ} \mathrm{C}$ is cooled at constant pressure until it exists as a compressed liquid at $20^{\circ} \mathrm{C}$.
(a) Show the process on a $T-\vee$ diagram with respect to saturation lines.
(b) Determine the change in volume.
(c) Find the change in total internal energy.

Answers: (b) $-0.187 \mathrm{~m}^{3},(c)-1984 \mathrm{~kJ}$
3-122 A $0.5-\mathrm{m}^{3}$ rigid tank containing hydrogen at $20^{\circ} \mathrm{C}$ and 600 kPa is connected by a valve to another $0.5-\mathrm{m}^{3}$ rigid tank that holds hydrogen at $30^{\circ} \mathrm{C}$ and 150 kPa . Now the valve is opened and the system is allowed to reach thermal equilibrium with the surroundings, which are at $15^{\circ} \mathrm{C}$. Determine the final pressure in the tank.


FIGURE P3-122
3-123 EGS Reconsider Prob. 3-122. Using EES (or other) software, investigate the effect of the surroundings temperature on the final equilibrium pressure in the tanks. Assume the surroundings temperature to vary from -10 to $30^{\circ} \mathrm{C}$. Plot the final pressure in the tanks versus the surroundings temperature, and discuss the results.
3-124 A $20-\mathrm{m}^{3}$ tank contains nitrogen at $23^{\circ} \mathrm{C}$ and 600 kPa . Some nitrogen is allowed to escape until the pressure in the tank drops to 400 kPa . If the temperature at this point is $20^{\circ} \mathrm{C}$, determine the amount of nitrogen that has escaped. Answer: 44.6 kg
3-125 Steam at $400^{\circ} \mathrm{C}$ has a specific volume of $0.02 \mathrm{~m}^{3} / \mathrm{kg}$. Determine the pressure of the steam based on (a) the idealgas equation, (b) the generalized compressibility chart, and (c) the steam tables. Answers: (a) $15,529 \mathrm{kPa}$, (b) $12,576 \mathrm{kPa}$, (c) $12,500 \mathrm{kPa}$

3-126 A tank whose volume is unknown is divided into two parts by a partition. One side of the tank contains $0.01 \mathrm{~m}^{3}$
of refrigerant-134a that is a saturated liquid at 0.8 MPa , while the other side is evacuated. The partition is now removed, and the refrigerant fills the entire tank. If the final state of the refrigerant is $20^{\circ} \mathrm{C}$ and 400 kPa , determine the volume of the tank.


FIGURE P3-126

3-127 EGS Reconsider Prob. 3-126. Using EES (or other) software, investigate the effect of the initial pressure of refrigerant-134a on the volume of the tank. Let the initial pressure vary from 0.5 to 1.5 MPa . Plot the volume of the tank versus the initial pressure, and discuss the results.
3-128 Liquid propane is commonly used as a fuel for heating homes, powering vehicles such as forklifts, and filling portable picnic tanks. Consider a propane tank that initially contains 5 L of liquid propane at the environment temperature of $20^{\circ} \mathrm{C}$. If a hole develops in the connecting tube of a propane tank and the propane starts to leak out, determine the temperature of propane when the pressure in the tank drops to 1 atm . Also, determine the total amount of heat transfer from the environment to the tank to vaporize the entire propane in the tank.


FIGURE P3-128

3-129 Repeat Prob. 3-128 for isobutane.
3-130 A tank contains helium at $100^{\circ} \mathrm{C}$ and 10 kPa gage. The helium is heated in a process by heat transfer from the surroundings such that the helium reaches a final equilibrium state at $300^{\circ} \mathrm{C}$. Determine the final gage pressure of the helium. Assume atmospheric pressure is 100 kPa .

3-131 A tank contains argon at $600^{\circ} \mathrm{C}$ and 200 kPa gage. The argon is cooled in a process by heat transfer to the surroundings such that the argon reaches a final equilibrium state at $300^{\circ} \mathrm{C}$. Determine the final gage pressure of the argon. Assume atmospheric pressure is 100 kPa .
3-132 Complete the blank cells in the following table of properties of steam. In the last column describe the condition of steam as compressed liquid, saturated mixture, superheated vapor, or insufficient information; and, if applicable, give the quality.

| P, kPa | T, ${ }^{\circ} \mathrm{C}$ | $\mathrm{v}, \mathrm{m}^{3} / \mathrm{kg}$ | $u, \mathrm{~kJ} / \mathrm{kg}$ | Condition description and quality (if applicable) |
| :---: | :---: | :---: | :---: | :---: |
| 200 | 30 |  |  |  |
| 270.3 | 130 |  |  |  |
|  | 400 | 1.5493 |  |  |
| 300 |  | 0.500 |  |  |
| 500 |  |  | 3084 |  |

3-133 Complete the blank cells in the following table of properties of refrigerant-134a. In the last column describe the condition of refrigerant-134a as compressed liquid, saturated mixture, superheated vapor, or insufficient information; and, if applicable, give the quality.

| P, kPa | $T,{ }^{\circ} \mathrm{C}$ | $\mathrm{v}, \mathrm{m}^{3} / \mathrm{kg}$ | $u, \mathrm{~kJ} / \mathrm{kg}$ | Condition description and quality (if applicable) |
| :---: | :---: | :---: | :---: | :---: |
| 320-12 |  |  |  |  |
| 100039.37 |  |  |  |  |
|  | 40 | 0.17794 |  |  |
| 180 |  | 0.0700 |  |  |
| 200 |  |  | 249 |  |

3-134 On the property diagrams indicated below, sketch (not to scale) with respect to the saturated liquid and saturated vapor lines and label the following processes and states for refrigerant-134a. Use arrows to indicate the direction of the process, and label the initial and final states:
(a) On the $P-V$ diagram sketch the constant temperature process through the state $P=280 \mathrm{kPa}, V=0.06 \mathrm{~m}^{3} / \mathrm{kg}$ as pressure changes from $P_{1}=400 \mathrm{kPa}$ to $P_{2}=200 \mathrm{kPa}$. Place the value of the temperature on the process curve on the $P-v$ diagram.
(b) On the $T-v$ diagram sketch the constant specific volume process through the state $T=20^{\circ} \mathrm{C}, v=0.02 \mathrm{~m}^{3} / \mathrm{kg}$ from $P_{1}=1200 \mathrm{kPa}$ to $P_{2}=300 \mathrm{kPa}$. For this data set place the temperature values at states 1 and 2 on its axis. Place the value of the specific volume on its axis.

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## Fundamentals of Engineering (FE) Exam Problems

3-135 A rigid tank contains 6 kg of an ideal gas at 3 atm and $40^{\circ} \mathrm{C}$. Now a valve is opened, and half of mass of the gas is allowed to escape. If the final pressure in the tank is 2.2 atm , the final temperature in the tank is
(a) $186^{\circ} \mathrm{C}$
(b) $59^{\circ}$
(c) $-43^{\circ} \mathrm{C}$
(d) $20^{\circ} \mathrm{C}$
(e) $230^{\circ} \mathrm{C}$

3-136 The pressure of an automobile tire is measured to be 190 kPa (gage) before a trip and 215 kPa (gage) after the trip at a location where the atmospheric pressure is 95 kPa . If the temperature of air in the tire before the trip is $25^{\circ} \mathrm{C}$, the air temperature after the trip is
(a) $51.1^{\circ} \mathrm{C}$
(b) $64.2^{\circ} \mathrm{C}$
(c) $27.2^{\circ} \mathrm{C}$
(d) $28.3^{\circ} \mathrm{C}$
(e) $25.0^{\circ} \mathrm{C}$

3-137 A $300-\mathrm{m}^{3}$ rigid tank is filled with saturated liquidvapor mixture of water at 200 kPa . If 25 percent of the mass is liquid and 75 percent of the mass is vapor, the total mass in the tank is
(a) 451 kg
(b) 556 kg
(c) 300 kg
(d) 331 kg
(e) 195 kg

3-138 Water is boiled at 1 atm pressure in a coffee maker equipped with an immersion-type electric heating element. The coffee maker initially contains 1 kg of water. Once boiling started, it is observed that half of the water in the coffee maker evaporated in 18 minutes. If the heat loss from the coffee maker is negligible, the power rating of the heating element is
(a) 0.90 kW
(d) 1.05 kW
(b) 1.52 kW
(e) 1.24 kW
(c) 2.09 kW

3-139 A $1-\mathrm{m}^{3}$ rigid tank contains 10 kg of water (in any phase or phases) at $160^{\circ} \mathrm{C}$. The pressure in the tank is
(a) 738 kPa
(d) 2000 MPa
(b) 618 kPa
(e) 1618 kPa
(c) 370 kPa

3-140 Water is boiling at 1 atm pressure in a stainless steel pan on an electric range. It is observed that 2 kg of liquid water evaporates in 30 min . The rate of heat transfer to the water is
(a) 2.51 kW
(d) 0.47 kW
(b) 2.32 kW
(e) 3.12 kW
(c) 2.97 kW

3-141 Water is boiled in a pan on a stove at sea level. During 10 min of boiling, it is observed that 200 g of water has evaporated. Then the rate of heat transfer to the water is
(a) $0.84 \mathrm{~kJ} / \mathrm{min}$
(d) $53.5 \mathrm{~kJ} / \mathrm{min}$
(b) $45.1 \mathrm{~kJ} / \mathrm{min}$
(e) $225.7 \mathrm{~kJ} / \mathrm{min}$

3-142 A $3-\mathrm{m}^{3}$ rigid vessel contains steam at 10 MPa and $500^{\circ} \mathrm{C}$. The mass of the steam is
(a) 3.0 kg
(b) 19 kg
(c) 84 kg
(d) 91 kg
(e) 130 kg

3-143 Consider a sealed can that is filled with refrigerant134a. The contents of the can are at the room temperature of $25^{\circ} \mathrm{C}$. Now a leak develops, and the pressure in the can drops to the local atmospheric pressure of 90 kPa . The temperature of the refrigerant in the can is expected to drop to (rounded to the nearest integer)
(a) $0^{\circ} \mathrm{C}$
(b) $-29^{\circ} \mathrm{C}$
(c) $-16^{\circ} \mathrm{C}$
(d) $5^{\circ} \mathrm{C}$
(e) $25^{\circ} \mathrm{C}$

## Design, Essay, and Experiment Problems

3-144 A solid normally absorbs heat as it melts, but there is a known exception at temperatures close to absolute zero. Find out which solid it is and give a physical explanation for it.
3-145 It is well known that water freezes at $0^{\circ} \mathrm{C}$ at atmospheric pressure. The mixture of liquid water and ice at $0^{\circ} \mathrm{C}$ is said to be at stable equilibrium since it cannot undergo any changes when it is isolated from its surroundings. However, when water is free of impurities and the inner surfaces of the container are smooth, the temperature of water can be lowered to $-2^{\circ} \mathrm{C}$ or even lower without any formation of ice at atmospheric pressure. But at that state even a small disturbance can initiate the formation of ice abruptly, and the water temperature stabilizes at $0^{\circ} \mathrm{C}$ following this sudden change. The water at $-2^{\circ} \mathrm{C}$ is said to be in a metastable state. Write an essay on metastable states and discuss how they differ from stable equilibrium states.
3-146 Enthalpy of Fusion for Water Experiment. The enthalpy of fusion for water (also known as latent heat of fusion) is obtained with an ice calorimeter that is constructed from a copper tube with closed ends and two access ports. Inside the calorimeter is coiled thermocouple wire that serves as electric heater wire. The calorimeter is filled with water, placed in a freezer and removed after the water is frozen. The calorimeter is insulated with Styrofoam and placed in a chamber with double walls that hold crushed ice and water providing a $0^{\circ} \mathrm{C}$ air environment. Electrical power input into the heater causes the solid ice at $0^{\circ} \mathrm{C}$ to melt to liquid water at $0^{\circ} \mathrm{C}$ - the energy supplied for this phase-change is the enthalpy of fusion. Obtain the enthalpy of fusion for water using the video clip, the complete write-up, and the data provided on the DVD accompanying this book.


[^0]:    Source: Data from National Bureau of Standards (U.S.) Circ., 500 (1952).

[^1]:    © Reprinted with special permission of King Features Syndicate.

[^2]:    *This section can be skipped without a loss in continuity.

[^3]:    *Problems designated by a "C" are concept questions, and students are encouraged to answer them all. Problems designated by an "E" are in English units, and the SI users can ignore them. Problems with a CD-EES icon are solved using EES, and complete solutions together with parametric studies are included on the enclosed DVD. Problems with a computer-EES icon are comprehensive in nature, and are intended to be solved with a computer, preferably using the EES software that accompanies this text.

